

Initiation de la décharge : *Discussion RPF 2020*

Théorie de l'ionisation directe dans le liquide

Formation d'une région de faible densité

Microbulles preexistantes

Théorie de Lewis – formation de cracks 1998

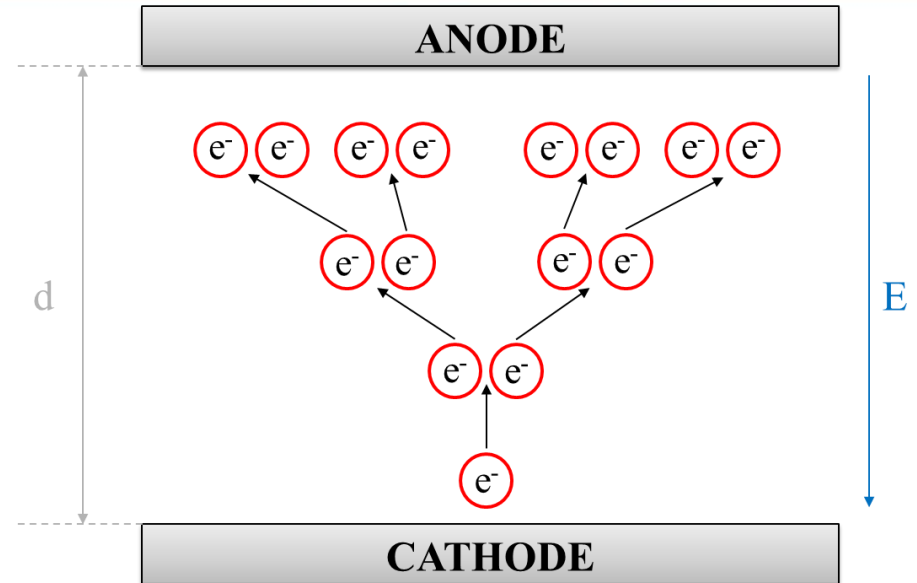
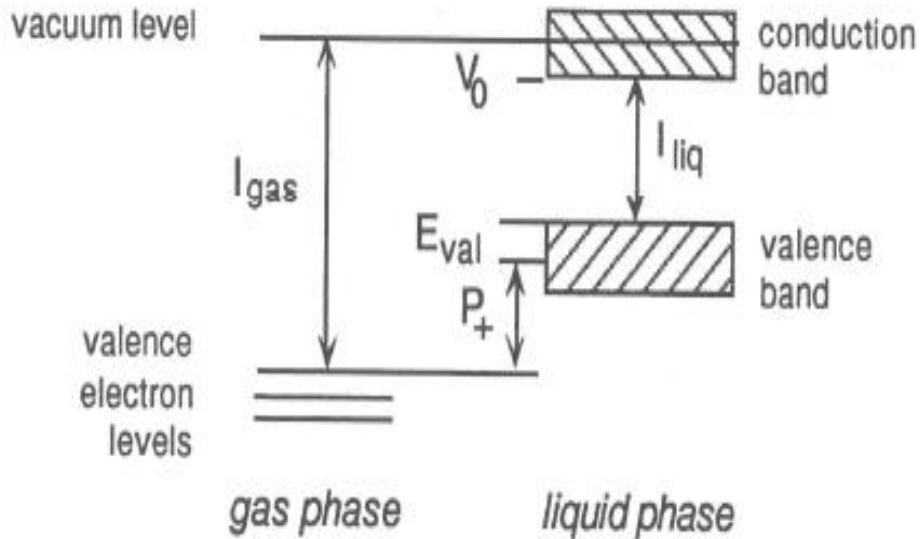
Théorie de l'électrostriction :
formation de nanopores
(cavité vide)

EHD Théorie O. Lesaint

.....

Initiation de la décharge : Discussion RPF 2020

Liquide



“The liquefied noble gases (Ar, Kr and Xe, at least) exhibit a band structure of electronic states, so that the atomic ionization potential should be replaced by the band gap, I_{liq} ”

Electron mean free path

$$l = \frac{1}{4\sigma N}$$

$$eEl$$

Gas

$$2 \cdot 10^{19} \text{ cm}^{-3}$$

liquid

$$2 \cdot 10^{22} \text{ cm}^{-3}$$

Rare Gas Liquid Detectors

Liquid	T(K)	$\mu_{el} \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$	I liq - Eg (eV)	free electron lifetimes	
Ar	85	475-625	14,3	>4 msec 0,1ppb of O2	Quasi-free
Kr	117	1800	11,7		
Xe	165	2950-2000	9,22+-0,01		
Methane	111	400			
Tetramethylsilane	295	99		100-200 μ s CERN TMP	
Neopentane	295	65			
Ethane	296	47			
Isooctane	296	7			
He	4.2	$2 \cdot 10^{-2}$	25,5		Electron bubble 17 Å
Cyclohexane	296	0.4			Localized
N pentane	296	0.16			
Water	293	$18 \cdot 10^{-4}$			Localized (solvated)

W F Schmidt
Liquid State Electronics of
Insulating Liquids 1997

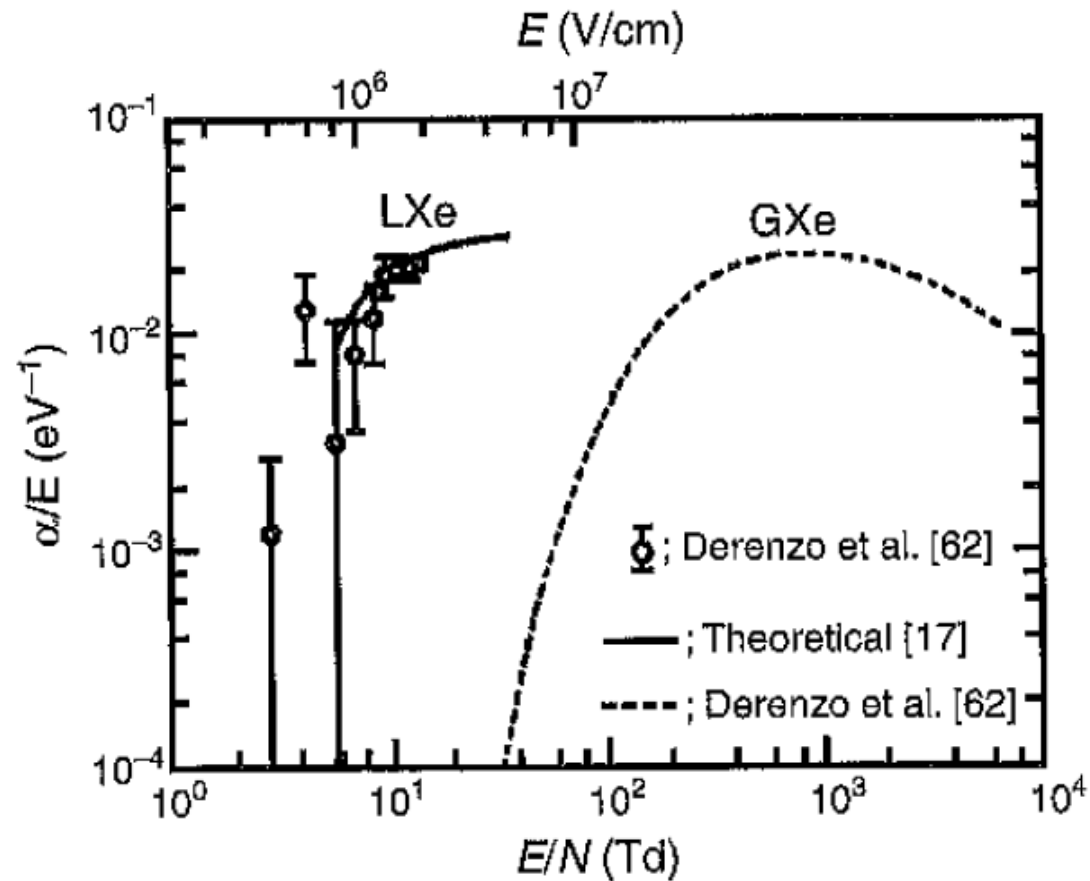
Electronic Excitations
in Liquefied Rare Gases 2005

Derenzo et al Phys. Rev. A 9, 2582 1974

First Townsend
coefficient α

Xe « pur »

20 cm



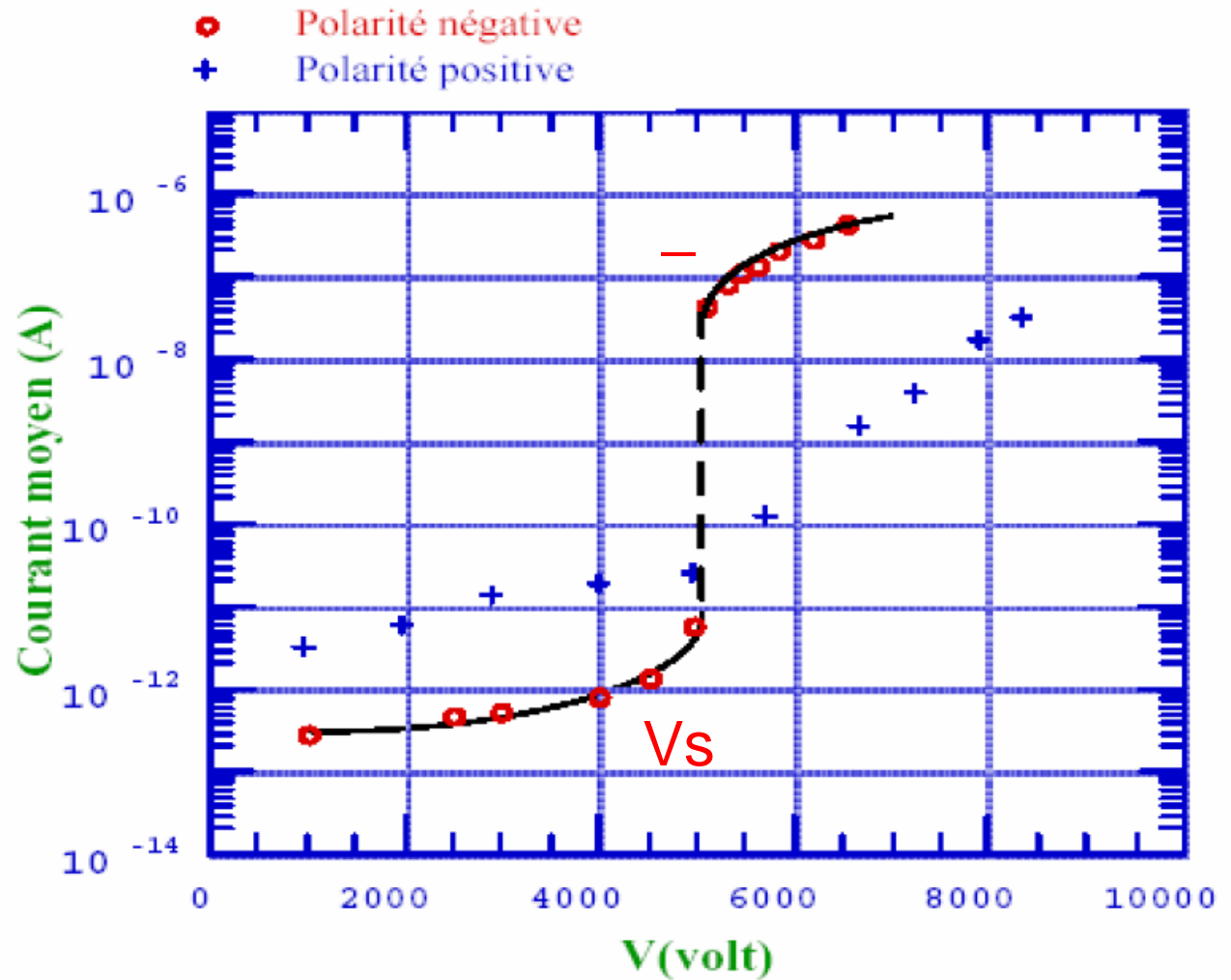
*Initiation de la décharge :
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*Experiences G2E.lab
Cyclohexane « purifié »*



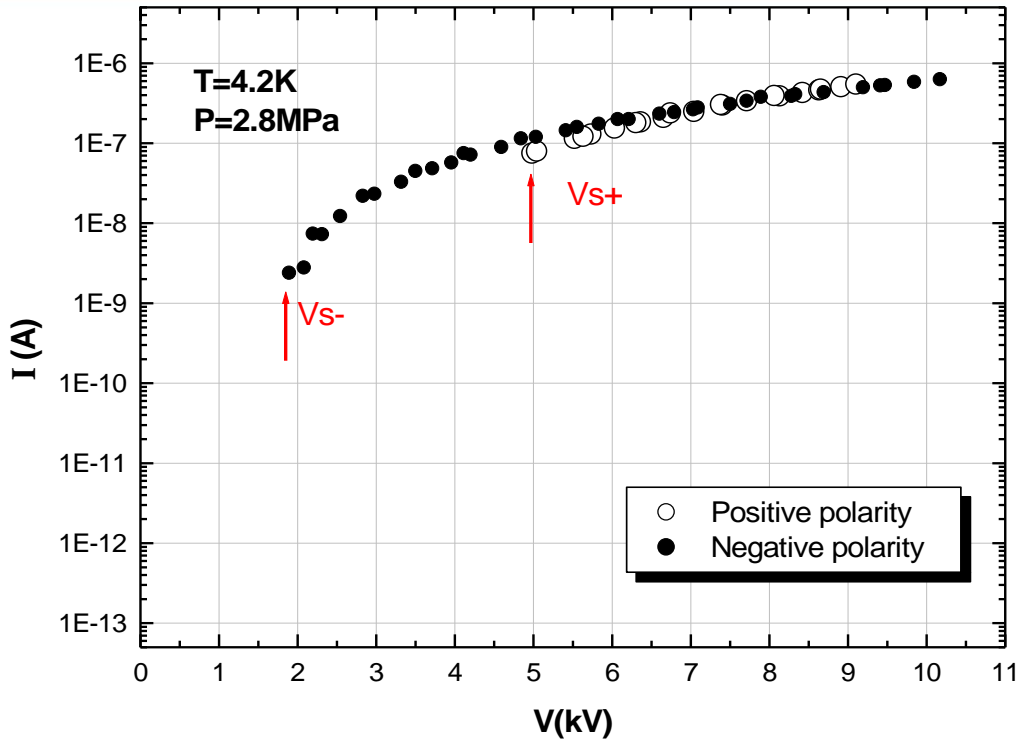
DC -/+
Pointe 0,1-2 μ m

courant résiduel



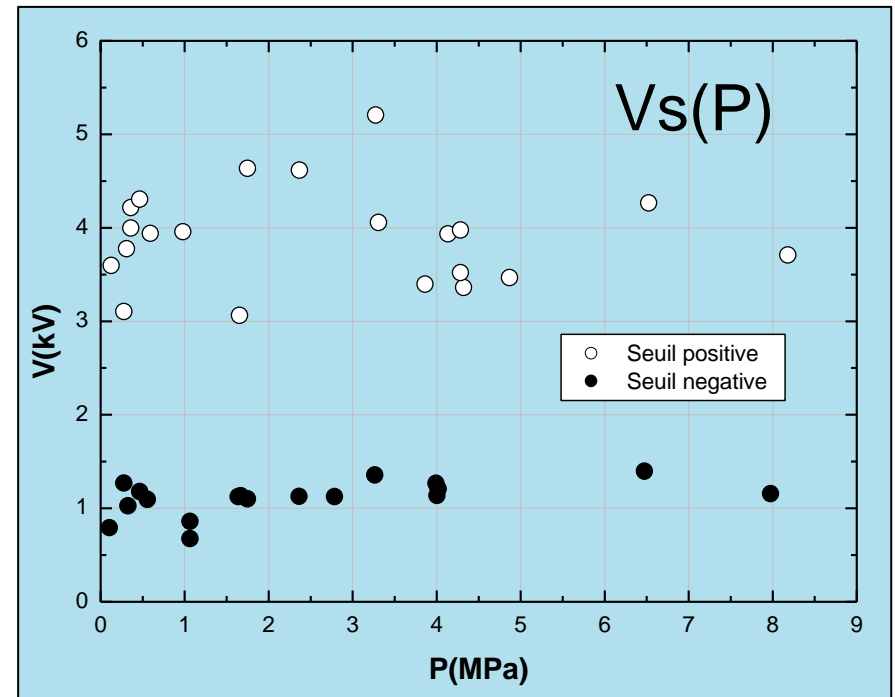
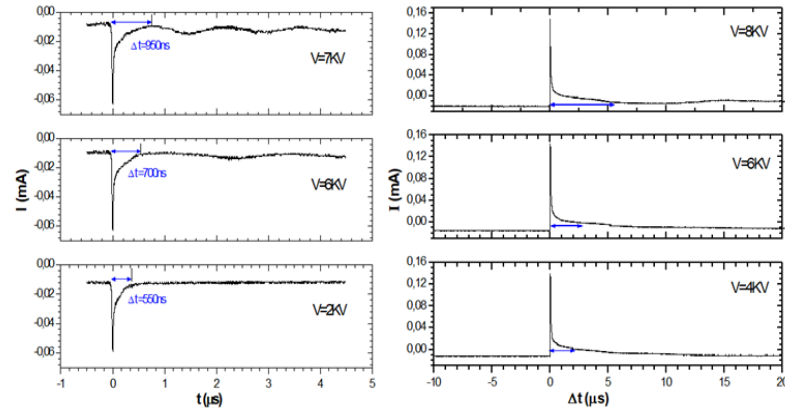
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Helium - Argon liquide



Courant résiduel

Vs is independent
of external pressure



*Initiation de la décharge :
Discussion RPF 2020*

Théorie de l'ionisation directe
dans le liquide

Formation d'une région
de faible densité

Application de la spectroscopie à l'étude des décharges électriques dans les milieux denses.

N Bonifaci

CNRS, G2Elab, F-38000Grenoble, France

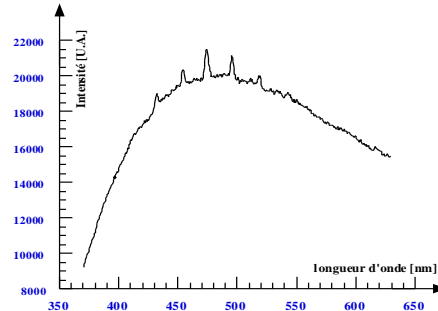
Nelly.Bonifaci@g2elab.grenoble-inp.fr

Joel Rosato, Sylvain Iséni, Jussi Eloranta, Olivier Lesaint,
Zhiling Li , Vladimir Atrazhev, Yann Cressault, Nader Sadeghi.

OES

$(T_e, T_k, T_{rot}, T_{vib}, T_{ex})$

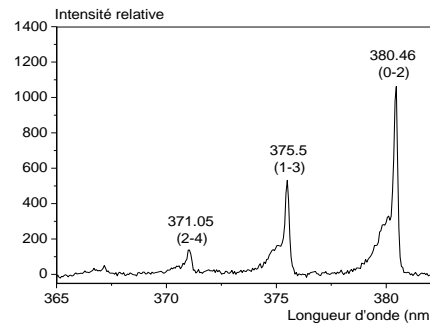
- Continuum



Theoretical background of optical emission spectroscopy for analysis of atmospheric pressure plasmas
T. Belmonte, C. Noël, T. Gries, J. Martin and G. Henrion, Plasma Sources Sci. Technol. 24, 064003 (2015).

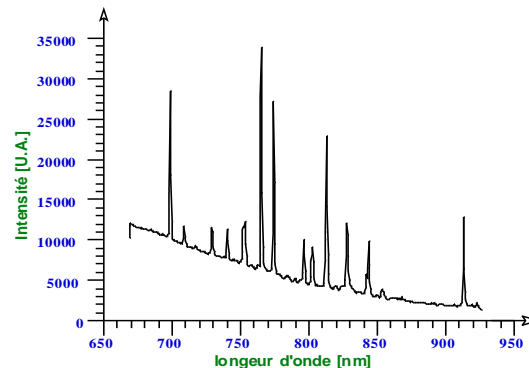
Présentation RPF 2020 Yann Cressault
Laboratoire LAPLACE, Toulouse

- Molecular spectra



Présentation RPF 2020 Yann Cressault
Laboratoire LAPLACE, Toulouse

- Atomic spectra



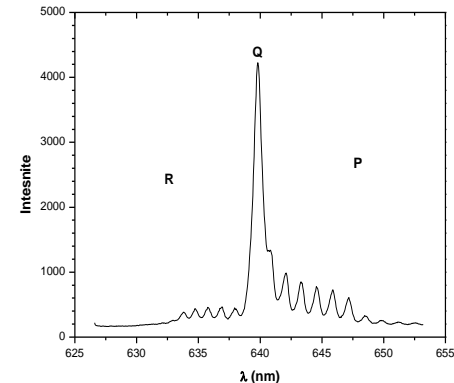
Molecular spectra

T_e : electronic term, $G(v)$: vibrational term, $F_v(J)$: terme rotationnel

$$G(v) = \omega_e \left(v + \frac{1}{2} \right) - \omega_e x_e \left(v + \frac{1}{2} \right)^2 + \omega_e y_e \left(v + \frac{1}{2} \right)^3 + \dots$$

$$F_v(J) = B_v J(J+1) - D_v J^2(J+1)^2 + \dots$$

J rotational quantum number



If the rotational states are in equilibrium they are distributed according to a Boltzmann law:

$$N_u = \frac{N_0 g_u}{Q(T_r)} e^{-E_u/kT_r}$$

T_r, T_v, \dots

B. Pearse and A. G. Gaydon

The identification of Molecular Spectra Chapman and Hall 1976

G. Herzberg, Molecular Spectra and Molecular Structure:

I. Spectra of Diatomic Molecules, 2nd edn.

(Van Nostrand, Princeton, NJ, 1950)

I. Kovacs, Rotational structure in the spectra of diatomic molecules (Adam Higer Ltd., London, 1969)

Home made code

Présentation RPF 2020

Yann Cressault Laboratoire LAPLACE, Toulouse

Simulation de spectres radiatifs : une aide précieuse pour le diagnostic des plasmas

5. Conclusion : **et les logiciels?**

- **Multitude de logiciels**
- **Systèmes moléculaires disponibles ?**
- **Quels paramètres/constantes spectro ?**
- **Quel couplage ?**
- **Quelle fonction d'appareil ?**
- **Quelles hypothèses ???**

LIFBASE

TABLEAU 1.1 Molécules et systèmes traités dans le logiciel LIFBASE

Molécule	Transition	Système	v_{max}
OH	A-X	Violet	8
OD	A-X		3
NO	A-X	γ	5
	B-X	β	7
	C-X	δ	1
	D-X	ϵ	5
CH	A-X		3
	B-X		1
	C-X		2
CN	B-X	Violet	8
	A-X		3
CF	B-X		5
	A-X		2
SiH	A-X		2
N ₂ ⁺	B-X	Premier Négatif	6

SPECAIR

TABLEAU 1.2 Molécules et systèmes traités dans le logiciel SPECAIR

Molécule	Système	Version <i>demo</i>
OH	Violet	✓
	Meinel	×
C ₂	Swan	×
	Violet	✓
CN	Rouge	×
	Infrarouge, Quatrième Positif	✓
N ₂	Premier Positif, Second Positif	×
N ₂ ⁺	Meinel	×
	Premier Négatif	✓
NH	A-X	×
NO	Infrarouge, γ , β	✓
	δ , ϵ , β' , γ'	×
O ₂	Schumann-Runge	×
Raies atomiques	C, N, O	✓

SPARTRAN

TABLEAU 1.3 Molécules et systèmes traités dans le logiciel SPARTAN

Molécule	Système
CO ₂	Infrarouge
H ₂	Lyman, Werner
C ₂	Swan, Philips, Mulliken,
	Deslandres-D'Azambuja, Fox-Herzberg,
	Ballik-Ramsay
CN	Violet, Rouge
CO	Infrarouge, Quatrième Positif,
	Angstrom, Troisième Positif,
	Triplet, Asundi
CO ⁺	B-A, B-X, Comet Tail
N ₂	Premier Positif, Second Positif
N ₂ ⁺	Premier Négatif
NO	γ , β , δ , ϵ , β' , γ'
	Schumann-Runge,
O ₂	Schumann-Runge Continuum
Raies atomiques	H, C, C⁺, N, N⁺, O, O⁺, Ar, Ar⁺, Hg, Xe, Xe⁺
Photo-ionisation	H, C, C⁺, N, N⁺, O, O⁺, Ar, Ar⁺, CO₂, C₂, N₂, O₂, CO, CN, NO
Photo-détachement	C⁻, N⁻, O⁻
Bremsstrahlung	N, O, N₂, O₂

MASSIVE OES

TABLEAU 1.4 Systèmes traités dans le logiciel massiveOES

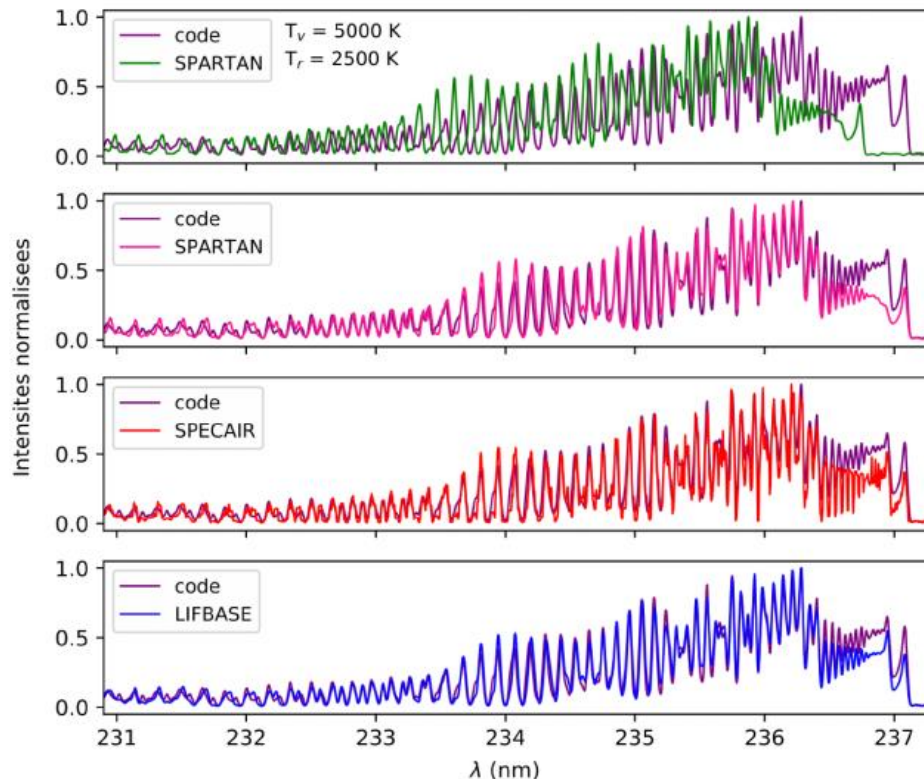
Molécule	Transition	Système	Base de données	Réfs.
N ₂ ⁺	B-X	Premier Négatif	LIFBASE	[LC99a]
OH	A-X	Violet	LIFBASE	[LC99a]
N ₂	C-B	Second Positif	→	[LK92], [FS98], [Nas+04]
NH	A-X		PGOPHER	[Ler73], [SPS94], [RB10], [Wes17]
NO	B-X	β	LIFBASE	[LC99a]

Présentation RPF 2020

Yann Cressault Laboratoire LAPLACE, Toulouse

Simulation de spectres radiatifs : une aide précieuse pour le diagnostic des plasmas

5. Conclusion : **et les logiciels?**



Ar-N₂, 1atm (A-M Kassir, PhD Thesis, 2020)



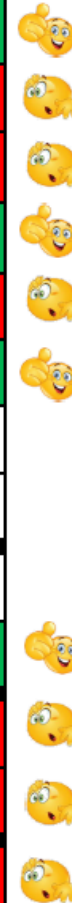
Système γ du radical NO
Cas d'un plasma thermique



Quand ca marche pas !!!

- Décalage en longueur d'onde de 0.235 nm ;
- Pas de dédoublement Λ dans l'état $^2\Pi$.
- Cas de couplage de Hund considéré pour le niveau fondamental ;
- Facteurs de Hönl-London différents.

	LIFBASE	SPECAIR	SPARTAN	Concordance
NO γ (A—X)	included	included	Included	Green
NO β (B—X)	included	included	Included	Red
NO δ (C—X)	included	included	Included	Red
NO ϵ (D—X)	included	included	Included	Green
NO β' (B'—X)	-	included	Included	Red
NO γ' (E—X)	-	included	Included	Green
NO 11000 Å (D—A)	-	included	-	-
NO Infrarouge (X—X)	-	included	-	-
N_2^+ Meinel (A—X)	-	included	-	-
N_2^+ Premier Négatif (B—X)	included	included	Included	Green
N_2 Premier Positif (B—A)	-	included	Included	Red
N_2 Second Positif (C—B)	-	included	Included	Red
O_2 Schumann-Runge (B—X)	-	included	Included	Red



Laplace
Etude des molécules diatomiques
C-H-O-N

- Comparaisons des logiciels
- Etudes expérimentales

The rotational temperature of a molecule is often use as a probe of the gas temperature



Second positive band system N_2 (C-B)
Ultraviolet band system OH (A-X)
First negative band system N_2^+ (B-X)

$$Tr_{N_2} \neq Tr_{OH}$$

Collisional time
Radiative life time
Quenching

“.... *observing a rotational Boltzmann distribution is a necessary but not sufficient condition for assuming that the rotational distributions are in equilibrium with the gas kinetic temperature.**an overpopulation of high rotational states occurs*, which in the absence of thermalization of the rotational states would typically lead to a larger rotational temperature parameter in comparison with the gas temperature.”

P J Bruggeman Nader Sadeghi et al Plasma Sources Sci Technol 23 (2014) 023001

Two « Temperatures » Model – 3 T
Boltzmann Plot

Spectral Line Profile $P_e(\lambda)$

$$\epsilon_\lambda = \frac{hc}{4\pi\lambda_{ul}} A_{ul} P_e(\lambda) N_u$$

$$h\nu_{ul} = \frac{h\omega_{ul}}{2\pi} = \frac{hc}{\lambda_{ul}} = E_u - E_l$$

A_{ul} : Einstein transition probability of spontaneous emission [s^{-1}],

h : Planck constant,

λ the wavelength of the emitted photon [m^{-1}].

N_u : number density of emitting species [m^{-3}] in the u state.

R. Stringanow and N. S. Sventitskii, Tables of Spectral Lines of Neutral and Ionized Atoms Plenum New York 1968.

NIST ASD Output: Lines <http://physics.nist.gov/cgi-bin/ASD/lines1.pl>

Atomic Spectral Line Database <http://cfa-www.harvard.edu/> (~~O I 777nm~~) (Cu I)

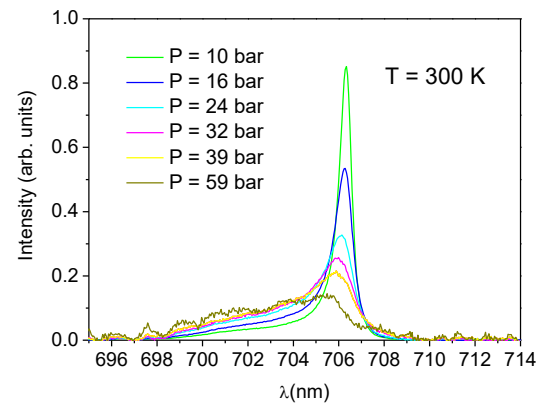
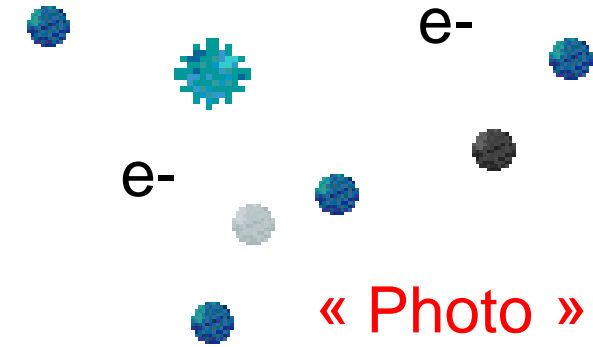
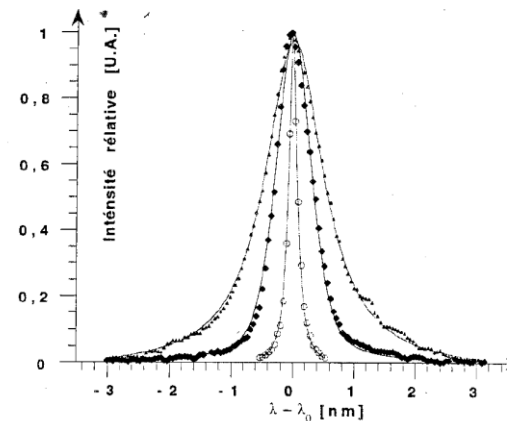
Spectral Line Profile $P_e(\lambda)$

Line width $\Delta\lambda_{FWHM}$
Line shift $d = \lambda_{max} - \lambda_{vacuum}$

FWHM : Full Width at Half Maximum

Asymmetry
Satellite band
Forbidden line
Self-absorption

Microscopic probe



Broadening mechanisms

Natural Broadening

$$\Delta\lambda_{\text{natural}} \sim 10^{-4} \text{ \AA}$$

Doppler Broadening

$$\Delta\lambda_D = 2\lambda \sqrt{\frac{2kT \ln 2}{Mc^2}} = 7.157 \times 10^{-7} \lambda \sqrt{\frac{T}{M}}$$

Gaussian Profile
Particle Temperature

	T	$\Delta\lambda_D$
He	10000	0,02 nm
Ar	10000	0,0057 nm
H $_{\beta}$	5000	0,025 nm

Instrumental Broadening

→ Gaussian profile

Pressure Broadening

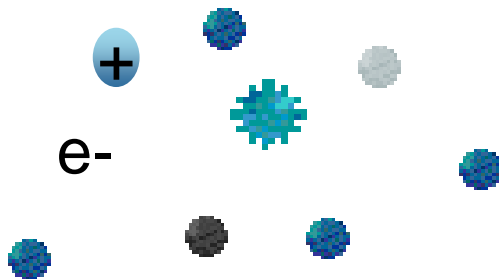
→ Lorentzian profile (Complex line)

Pressure Broadening

The radiation emitted from an atom is changed by the force field of a neighboring atom. Frequency and amplitude are therefore no longer constant in time. . . . The change is so great, however, that the phase of the vibration after the collision is no longer the same as it would have been had there been no collision.

—Weisskopf, 1933

Stark ($p=2,4$)
Neutral (van der Waals) ($p=6$)
Resonant ($p=3$)



Semi-empirical potential

$$V(r) = \pm \frac{\hbar C_p^\omega}{r^p} = \pm \frac{h C_p^v}{r^p} \quad 2\pi$$

$$m^p s^{-1}$$

ab-initio potential

Laboratoire de Chimie et Physique Quantiques
Systèmes ayant un faible nombre d'électrons

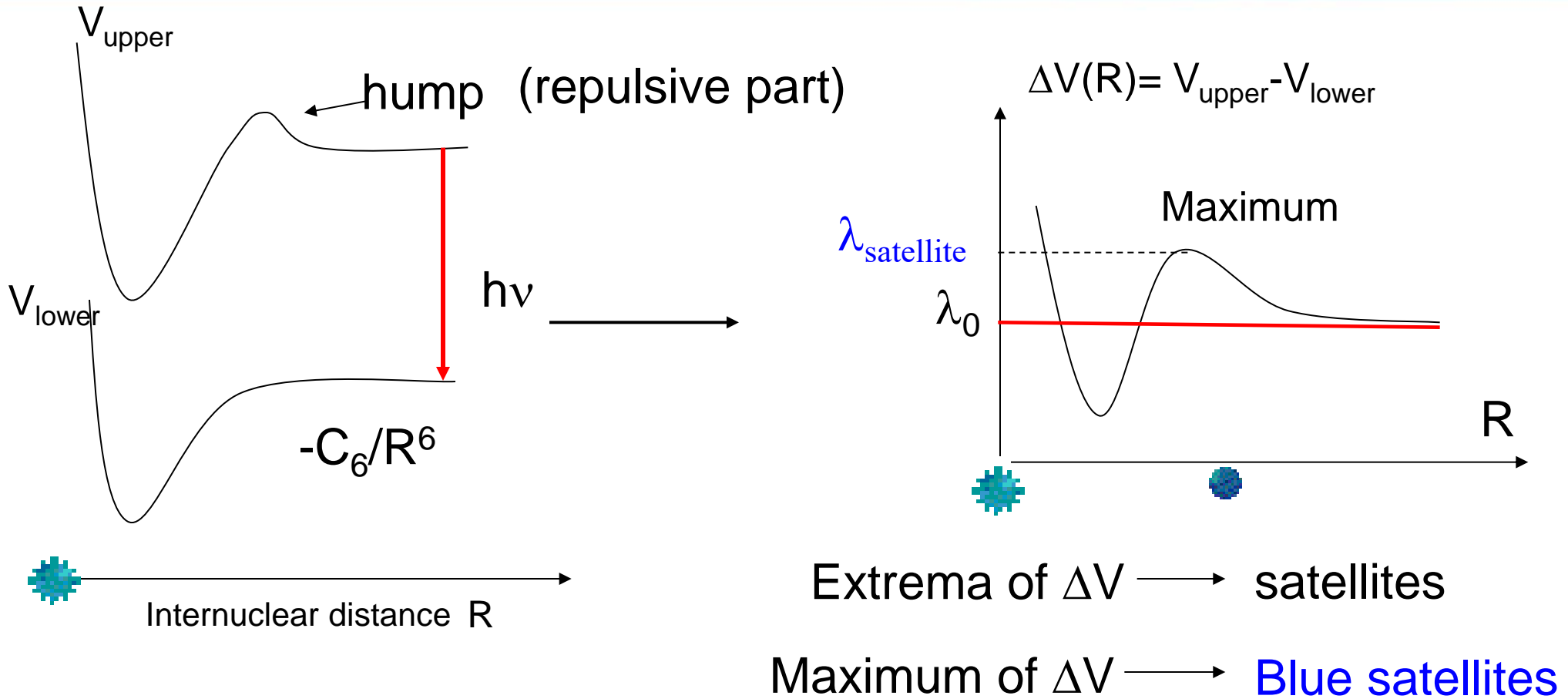
Semi-empirical Potential

Linear Stark	$V(r) = \pm \frac{\hbar C_2^\omega}{r^2}$	Literature
Quadratic Stark	$V(r) = \pm \frac{\hbar C_4^\omega}{r^4}$	Literature
Resonant	$V(r) = \pm \frac{\hbar C_3^\omega}{r^3}$	$C_3^\omega = \frac{e^2 f_r \lambda_r}{16\pi^2 \epsilon_0 m_e c}$
van der Waals	$V(r) = -\frac{\hbar C_6^\omega}{r^6}$	$C_6^\omega = \frac{1}{2h\epsilon_0} e^2 \alpha \left \langle r^2 \rangle \right \text{ m}^6\text{s}^{-1}$ $C_6^\omega = e^2 \alpha \left \langle r^2 \rangle \right \text{ ergcm}^6$ α atomic polarizability m^3 $\langle r^2 \rangle = a_0^2 \frac{n^{*2}}{2z_i^2} \langle 5n^{*2} + 1 - l(l+1) \rangle$ $n^* = \sqrt{z_i \frac{E_H}{E_i - E_u}}$
\Leftrightarrow	$V(r) = \hbar \left(\frac{C_{12}}{r^{12}} - \frac{C_6^\omega}{r^6} \right)$	W. Behmenburg J. Quant. Spectrosc. Radiat. Transfer 4, (1964) 177 W. R. Hindmarsh, A. D. Petford, G. Smith, Proc Roy Soc A 297 (1967) 296 W. R. Hindmarsh, A. N. Du Plessis et J. M. Farr (1970) J. Phys. B: At. Mol. Opt. Phys. 3, L5-L8 Butaux, F Schuller, R Lennuier J de Phys, 33, (1972), 635. ab initio potential

ab initio potential

H G Kuhn : Does your treatment predict satellite line?

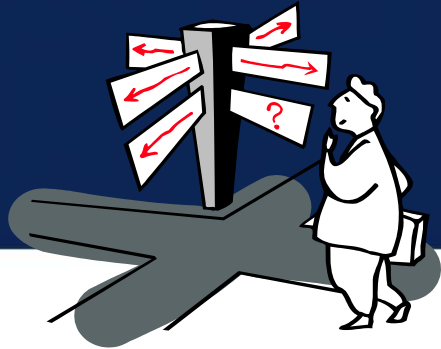
A Jablonski: The theory does not predict this mysterious effect. 1968



MOLPRO 2009 package

<http://www.molpro.net>

Laboratoire de Physique et Chimie Quantique Toulouse



Interaction Physical classification

Stark (Literature)
Van der Waals ($-C_6/r^6$)
Resonant ($\pm C_3/r^3$)

Potentiel ab initio

MOLPRO 2009 package
<http://www.molpro.net>

Spectral line Profile

Classical theory

?

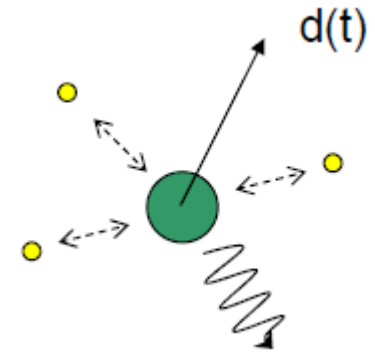
?

Quantum treatment

Stark

$$I(\omega) = \frac{1}{\pi} \operatorname{Re} \int_0^{\infty} dt \langle \vec{d}(0) \cdot \vec{d}(t) \rangle e^{i\omega t}$$

\vec{d} is the dipole moment



$U(t)$ evolution operator relative to the electrons

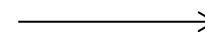
$$\vec{d}(t) = U^+(t) \vec{d}(0) U(t)$$

U-matrix

$$i\hbar \frac{dU}{dt}(t) = (H_0(t) + V(t))U(t)$$

H_0 is the Hamiltonian of the unperturbed emitter

time-dependent Schrödinger equation
for the evolution operator $U(t)$



Code

PIIM Marseille
Weizmann Institute of Science, Israel;
Valladolid Spain

Line shape formalism based on the Fourier transform of the autocorrelation function

$$P(\omega) = \frac{1}{\pi} \operatorname{Re} \int_0^{+\infty} \phi(\tau) \exp[i\omega\tau] d\tau \quad \phi(\tau) = \int_{-\infty}^{+\infty} e^{i(\eta(t) - \eta(t-\tau))} dt$$

$$\phi(\tau) = \left\langle e^{-i\eta} \right\rangle_t = e^{-N_{pert} V_p(\tau)}$$

Autocorrelation function (wave train)

The autocorrelation function measures the average evolution of the wave train over a time interval τ from an initial time t

P. W. Anderson, Phys Rev 76 (1949) 647.

P. W. Anderson, Phys Rev 86 (1952) 809.

Spectral Line Profile

Classical theory

$$\phi(\tau) = \left\langle e^{-i\eta} \right\rangle_t = e^{-N_{pert} V_p(\tau)}$$

Perturber density N_{pert}

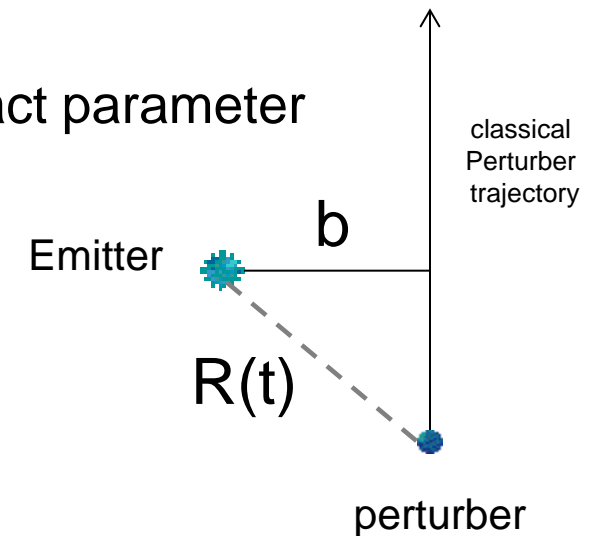
V_p : collision volume

$$V_p(\tau) = 2\pi \left[\int_0^{+\infty} b db \int_{-\infty}^{+\infty} dx \left\{ 1 - \exp\left(-i \frac{1}{\hbar} \int_0^{\tau} V(R(t')) dt'\right) \right\} \right]$$

Rectilinear classical path

$$R(t) = \left[b^2 + (x_0 + \bar{v}t)^2 \right]^{1/2}$$

b is the impact parameter



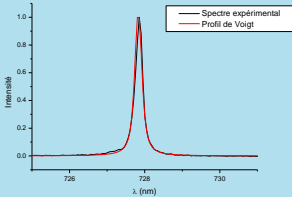
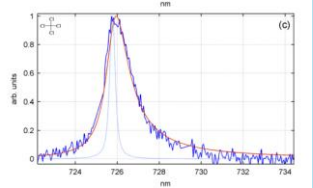
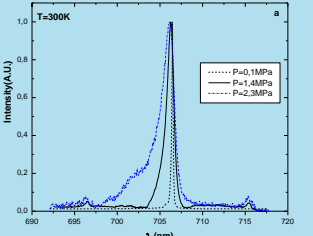
Unified theory

Impact approximation $N_{pert} \ll \ll$

Quasistatic approximation $N_{pert} \gg \gg$

Spectral Line Profile

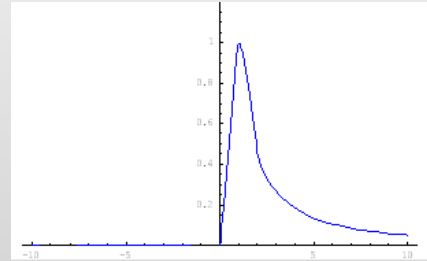
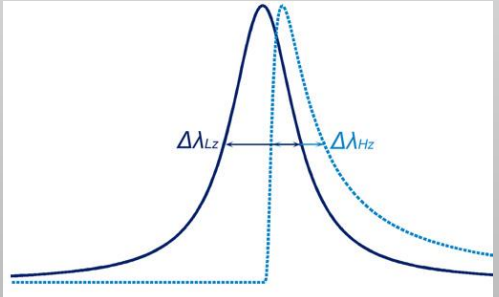
The quasistatic and impact approximations represent important theoretical limits that are in many cases sufficient for practical purposes and have been used to guide and develop new methods that are more generally applicable and, in fact, satisfactorily solve the line broadening problem in practically all cases. S. Alexiou / (2009)

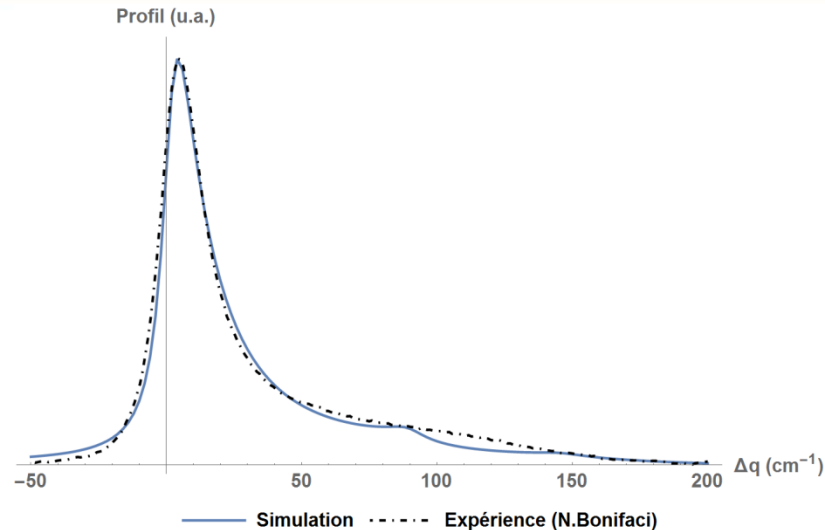
Experimental profile			
	<p>Lorentzian profile (Voigt profile)</p>	<p>Impact approximation</p>	<p>$N \ll \omega$, core</p>
	<p>Red Asymmetric profile</p>	<p>Quasi static approximation</p>	<p>$N \gg \omega$, wing</p>
	<p>Complex Satellite Blue wing</p>	<p>Unified theory (ab initio potential)</p>	<p>N, ω</p>

Impact approximation

Stark	literature
Resonant	$\Delta\lambda_{res} = K \frac{1}{\pi} \sqrt{\frac{g_0}{g_r}} \frac{e^2 \lambda_{ul}^2 f_r \lambda_r}{4\pi\epsilon_0 m_e c^2} N \propto \frac{P}{T}$ <p>K: 0,9-1,8</p> $S_{\lambda_{res}} \approx 0$
van der Waals	$\Delta\lambda_{vdw} = A \left(\frac{\lambda_{ul}^2}{2\pi c} \right) \Delta C_6^{2/5} \bar{v}^{-3/5} N \propto \frac{P}{T^{0.7}}$ <p>A : 8.08 ou 8.16</p> $S_{\lambda_{vdw}} = \frac{\Delta\lambda_{VDW}}{2,75} \quad \bar{v} = \sqrt{8kT/\pi\mu}$

Quasistatic Approximation

Stark	-----
Resonant	<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="background-color: #e0f0ff; padding: 5px;"> $\Delta\lambda_{resQS} = \Delta\lambda_{res} (1 - \beta N)$ </div> <div> $S_{\lambda res QS} \approx \epsilon \Delta\lambda_{res QS}$ </div> </div> <p style="text-align: center;">H. R. Zaidi , Can. J. Physics 55, (1977) 1243.</p>
Van der Waals	<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="background-color: #e0f0ff; padding: 5px;"> $\Delta\lambda_{QS} = 0.411\pi^2 C_6 \frac{\lambda_{ul}^2}{c} N^2$ </div> <div>  </div> </div> <div style="display: flex; justify-content: space-between; align-items: center; margin-top: 20px;"> <div style="font-size: 2em;">{</div> <div style="flex-grow: 1;"> $P_{QS}(\lambda) = \frac{1}{2} \left(\frac{\Delta\lambda_{qs}}{(\lambda - \lambda_{ul})^3} \right)^{1/2} \exp\left(-\frac{\pi}{4} \frac{\Delta\lambda_{qs}}{(\lambda - \lambda_{ul})} \right) \quad \lambda > \lambda_{ul}$ $P_{QS}(\lambda) = 0 \quad \lambda \leq \lambda_{ul}$ </div> </div> <div style="margin-top: 20px; text-align: center;"> $P_T = \int_{-\infty}^{+\infty} P_{Lor}(\Delta\lambda - \zeta) P_{QS}(\zeta) d\zeta$  </div> <p style="text-align: center;">H. Margenau Phys. Rev. 48, (1935) 755. H. Margenau Phys Rev 82 (1951) 156.</p>



Unified theory N Allard

GEPI, Observatoire de Paris

Ab initio potential

$$g_{(i,f)}(\tau) = \frac{1}{\sum_{ee'} \alpha |d_{ee'}|^2} \sum_{ee'} \alpha \int_0^{\infty} 2\pi\rho d\rho \int_{-\infty}^{+\infty} dx d_{ee'}(R(0)) \left[e^{\frac{i}{\hbar} \int_0^{\tau} dt \mathbf{V}(R(t))} \tilde{d}_{e'e}^*(R(\tau)) - \tilde{d}_{ee'}(R(0)) \right]$$

modulated electric dipole transition moment $\tilde{d}_{ee'}^0(R(t)) = d_{ee'}[R(t)] e^{-\frac{1}{kT} V_e[R(t)]}$

$d_{ee'}$ Dipole transition moment (ab initio calculation)

Stark broadening

Linear Stark effect Hydrogen lines

H_α 656.2 nm, H_β 486.1 nm

<p>H.R. Griem, Plasma Spectroscopy, Academic Press, New York, 1964.1964 H Griem Spectral line broadening by Plasmas London Academic 1974 H. Griem, Principles of Plasma Spectroscopy, Cambridge University Press, 1997.</p>	$N_e = C(N_e, T) * \Delta\lambda^{3/2}$ <p>Where $C(N_e, T)$ is in $A^{-3/2} cm^{-3}$.</p>
<p>M. Gigosos et V. Gardeñoso, J. Phys. B: At. Mol. Opt. Phys., vol. 29, no 20, p. 4795, oct. 1996.</p> <p>M. Gigosos , M Gonzalez V. Gardeñoso Spectrochimica Acta Part B 58 (2003) 1489–1504</p>	<p>H_α { Table full width at half area</p> $H_\beta \quad \Delta\lambda_{stark} (nm) = 4.8 \left(\frac{N_e}{10^{23}} \right)^{0.68116}$

Example : Helium Gas

Linear Stark effect + van der Waals

$$\Delta\lambda_{lor} = \Delta\lambda_{stark}(N_e, T_e) + \Delta\lambda_{vdw}(N)$$

H- β	C_6 [m ⁶ s ⁻¹]	$\Delta\lambda_{vdw}$
4s-2p	7.59*10 ⁻⁴³	2.20 × 10 ⁻⁵ PT ^{-7/10}
4p-2s	6.85*10 ⁻⁴³	2.12 × 10 ⁻⁵ PT ^{-7/10}
4d-2p	5.82*10 ⁻⁴³	1.98 × 10 ⁻⁵ PT ^{-7/10}

H- α	C_6 [m ⁶ s ⁻¹]	$\Delta\lambda_{vdw}$
3s-2p	2.75*10 ⁻⁴³	2.40 × 10 ⁻⁵ PT ^{-7/10}
3p-2s	1.696*10 ⁻⁴³	2.20 × 10 ⁻⁵ PT ^{-7/10}
3d-2p	1.18*10 ⁻⁴³	1.93 × 10 ⁻⁵ PT ^{-7/10}

H $_{\beta}$ quadratic Stark, H $_{\alpha}$ self –absorption

Quadratic Stark Effect

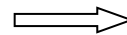
Impact Approximation

electrons

$$J(x) = \frac{1}{\pi} \int_0^{\infty} \frac{W(\beta) d\beta}{1 + (x - A^{4/3} \beta^2)^2}$$

$$\Delta\lambda_{Stark} = (1 + 1.75\alpha(1 - 0.75r)) 2\omega$$

$$S_{\lambda(Stark)} = d \pm 2A(1 - 0,75r)\omega$$



Quasistatic Approximation

ions

Holtsmark distribution

$$W(\beta) = (2/\pi) \beta \int_0^{\infty} \chi \sin(\beta\chi) \exp(-\chi^{3/2}) d\chi$$

N_e, T_e

p. 97 Griem 1974

- H. R. Griem (1964) Plasmas Spectroscopy , McGraw-Hill Book Compagny, New York.
- H .R. Griem (1974) Spectral Line Broadening by Plasmas , New York : Academic Press.
- H. R. Griem (1997) Principles of Plasma Spectroscopy , Cambridge.



Stark : Line shape Code

Quantum treatment, Numerical calculation



Simulation code	LSNS	PIIM Rosato, J. et al J. Quant. Spectrosc. Radiat. Transfer 2015 , 165, 102–107	computer simulation method The particle motion is simulated and the Schrödinger Eq. is solved numerically it is time consuming	
	SimU	Stambulchik, E. et al Phys. Rev. E 2007 , 75, 016401		
			
Models	PPP	PIIM Calisti, A et al Phys. Rev. A 1990 , 42, 5433–5440.	Frequency Fluctuation Model Rapid calculations for neutral and charged emitters	
	QC-FFM	Stambulchik, E. et al Phys. Rev. E 2013 , 87, 053108.	Frequency Fluctuation Model	
	Zest	Gilleron, F et al Atoms 2018 , 6, 11	Quasi-static description of ions and impact approximation for electrons	
			



Interaction Physical classification

Stark (*literature*)
 Van der Waals ($-C_6/r^6$)
 Resonant ($\pm C_3/r^3$)

Potentiel ab initio
 Code MOLPRO
<http://www.molpro.net>

Spectral line Profile

Classical theory

- Unified theory
- Impact approximation
- Quasistatic approximation

Quantum treatment

Stark

PIIM Marseille
 Weizmann Institute of Science, Israel;
 Valladolid Spain

Examples

Positive streamers in liquid nitrogen

Streamers in chlorinated alkane
and alkene liquids

Approximation quasi static

vdw

Corona discharge in Helium 300 K

Unified theory Ab initio potential

Quantum treatment Stark

Cold helium jet

2 T model

Corona discharge in Helium 4 K

→ ?

Positive filamentary streamers in liquid nitrogen

Two distinct phases

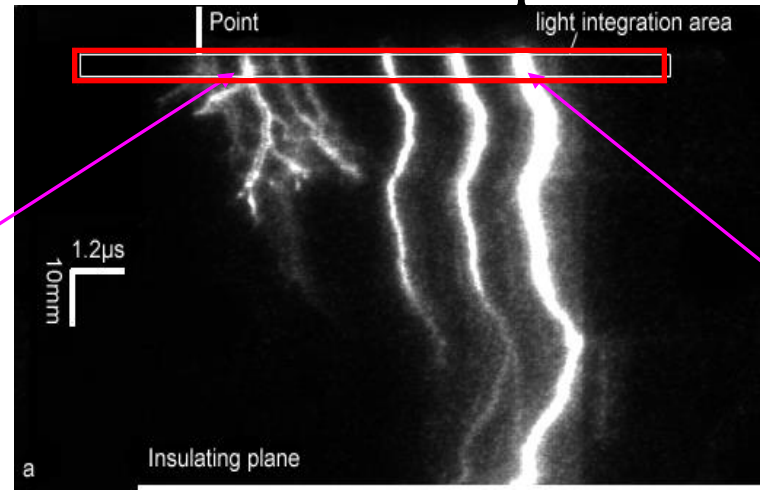
0,4/1400 μ s
100-200 mA

80mm, 102kV

The streamer propagation

Weak emitted light

~100 streamers

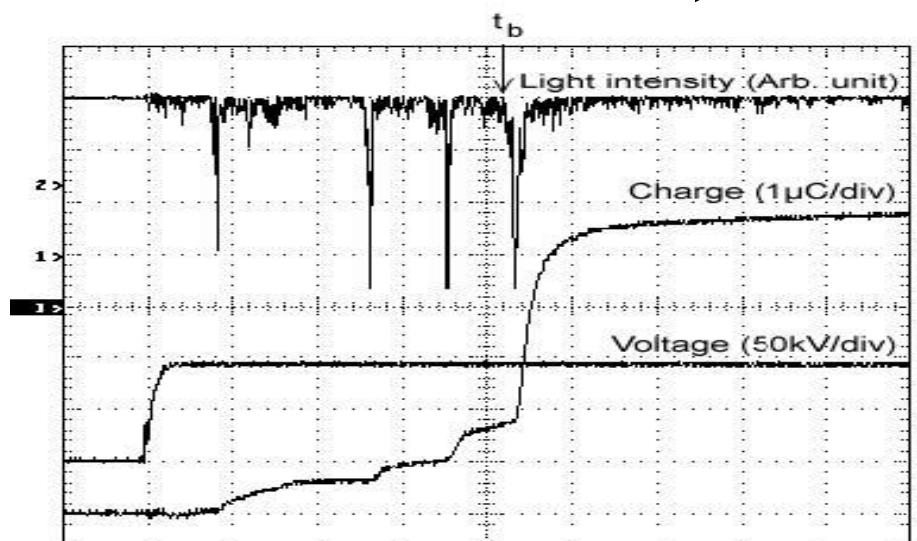


Streak photograph of filamentary streamer propagating up to plane

Streamer reaches the plane
Re-illumination

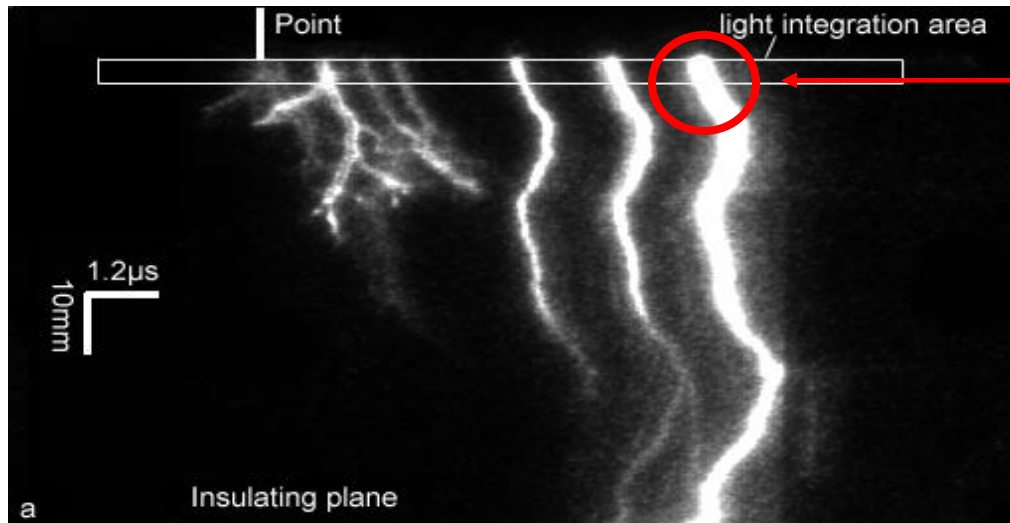
Intense emitted light

1 streamer



Experimental Results

Re-illumination



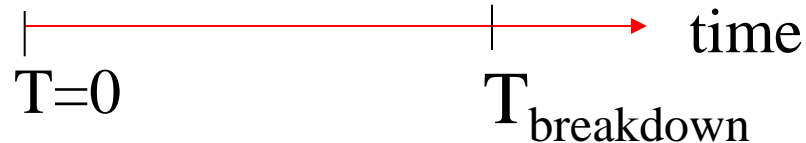
Light emitted by **one** positive streamer in LN₂ when it stops on the insulating plane

Intense NI Atomic line

(3s⁴P-3p⁴S⁰ and 3s⁴P-3p⁴P transition)



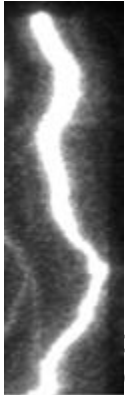
No N₂ emission



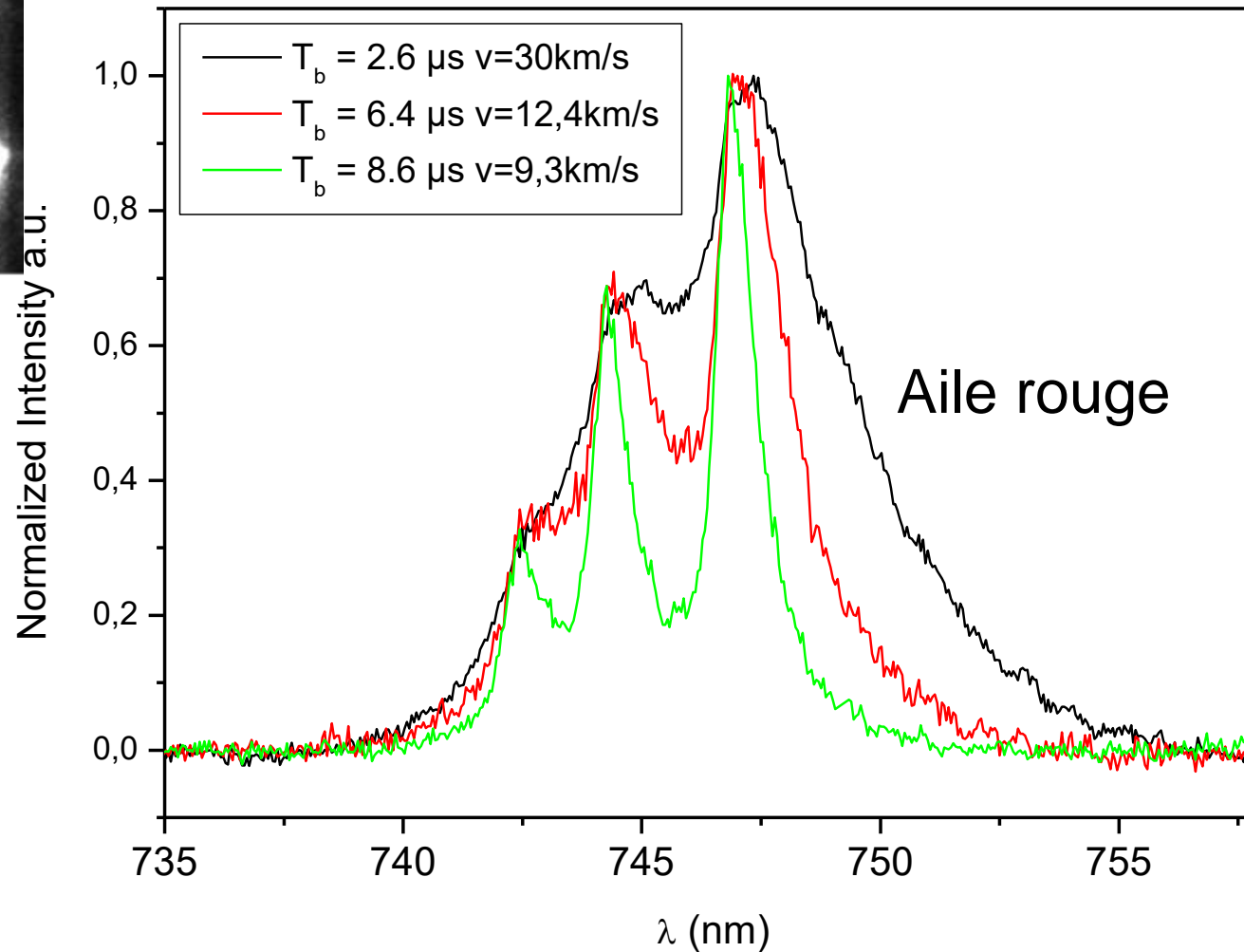
When one positive streamer stops on the insulating plane, a large current pulse and a bright emitted light are recorded at t_b

Positive filamentary streamers in liquid nitrogen

Re-illumination

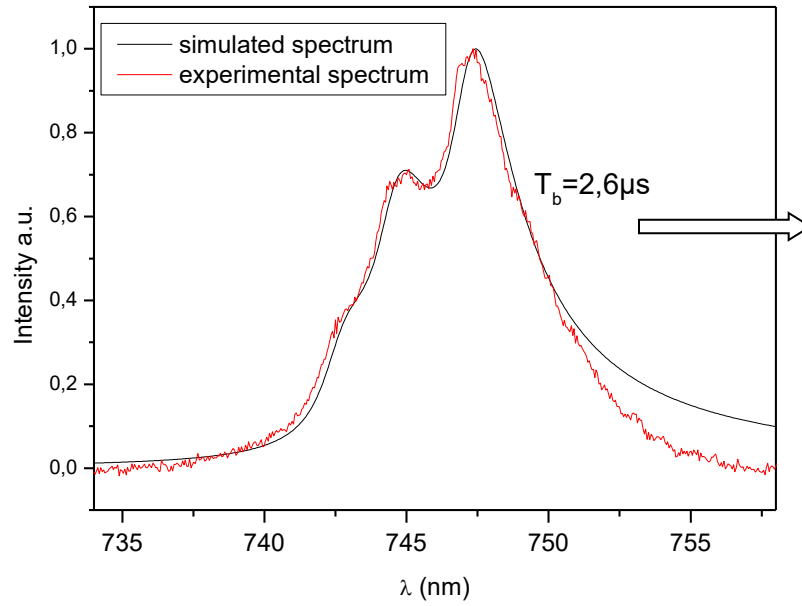
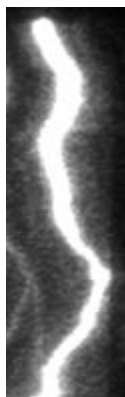


Propagation velocity : 10-30 km/s



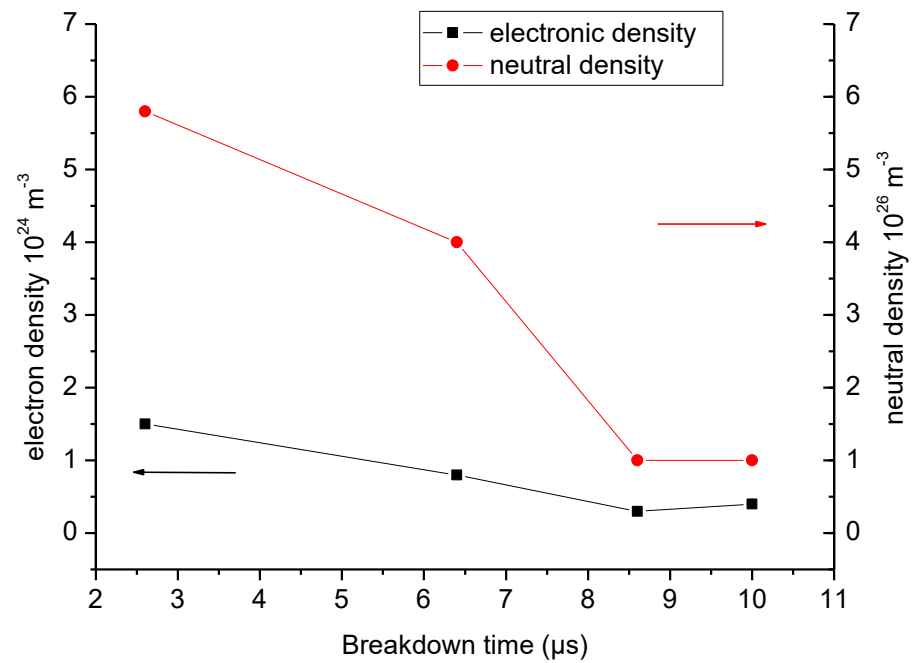
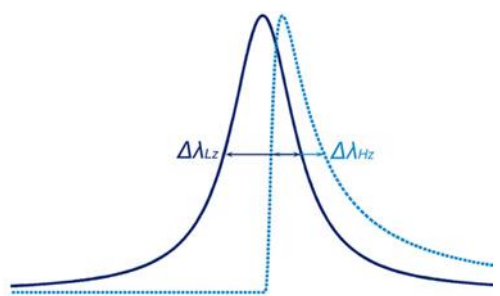
Broadening of Atomic line of NI ($3s^4P-3p^4P$)

Positive filamentary streamers in liquid nitrogen

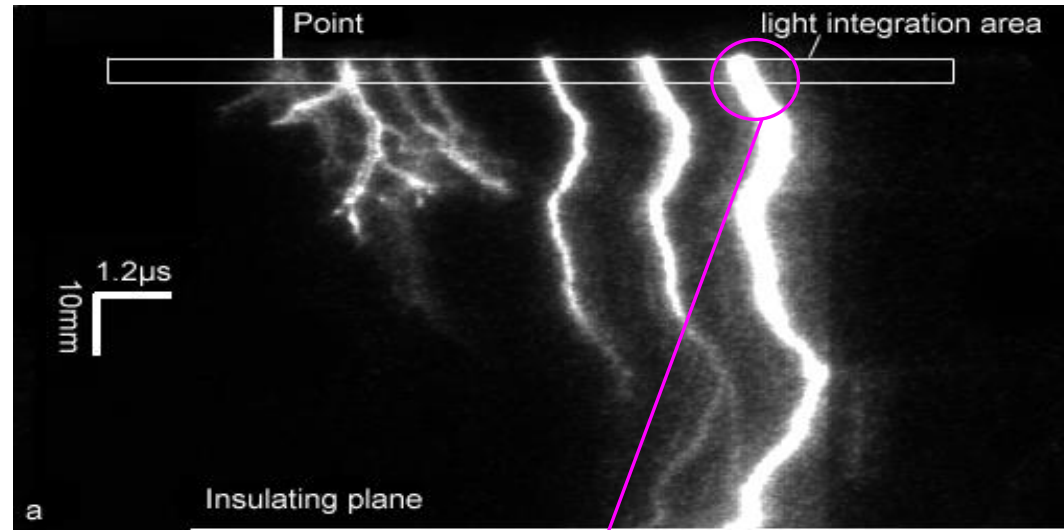


$N_e \sim 1,5 \times 10^{24} \text{ m}^{-3}$
 $N_g \sim 6 \times 10^{26} \text{ m}^{-3}$

Quasi static approximation



Positive filamentary streamers in liquid nitrogen



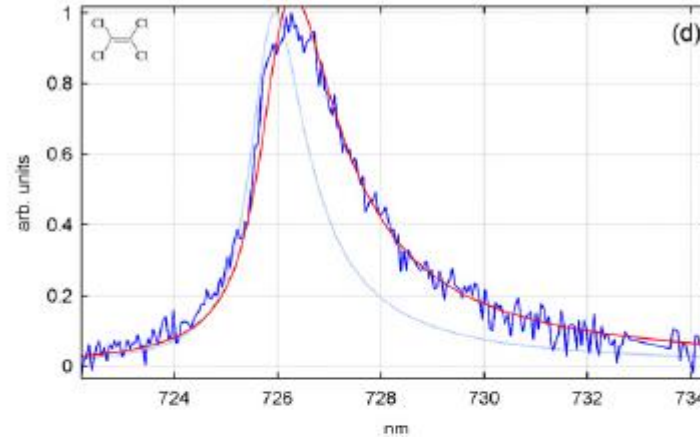
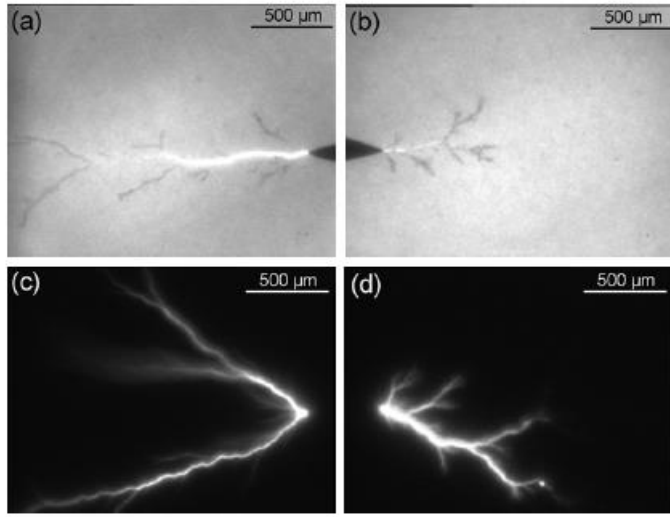
2000 K- 3000 K

Internal Pressure of the gas ~ 200 B $V=30$ km/s

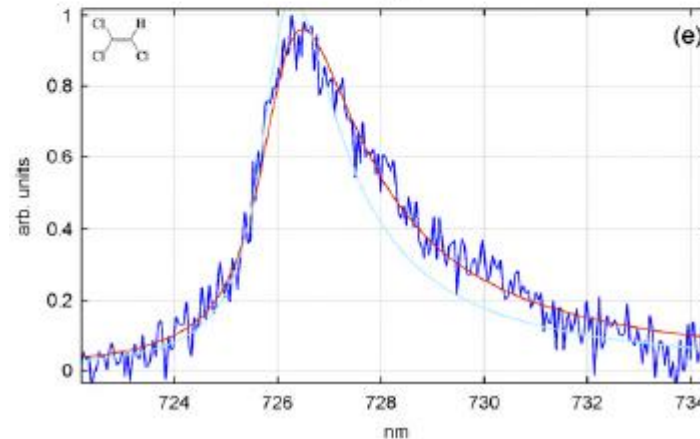
Internal Pressure of the gas ~ 30 B $V=10$ km/s

$N_e=0,5-1,5 \cdot 10^{24} \text{ m}^{-3}$

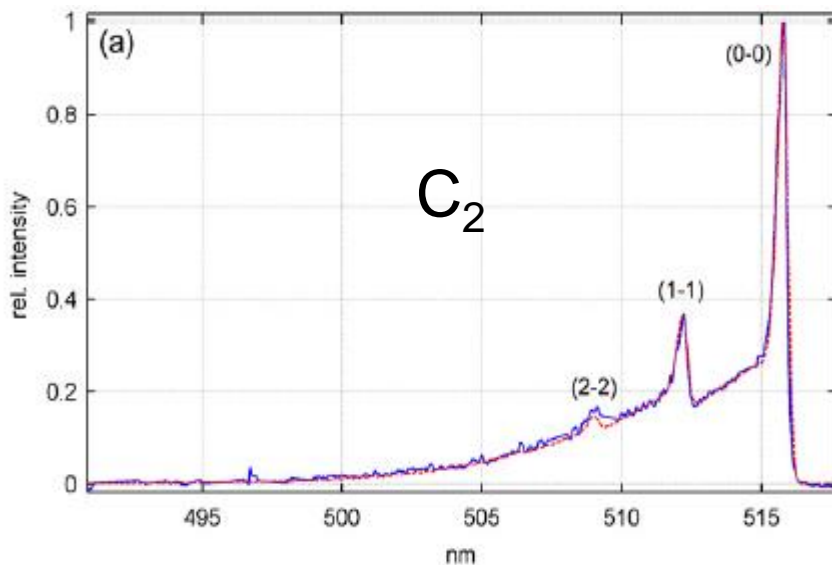
Streamers in chlorinated alkane and alkene liquids



725,6 nm



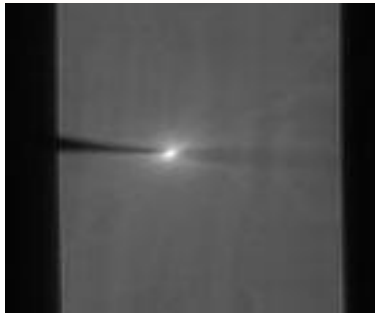
20-30 km/s



$T_{\text{rot}} = 3000-4000 \text{ K}$
 $P = 86-136 \text{ bar}$
 $N_e = 4-8 \cdot 10^{23} \text{ m}^{-3}$

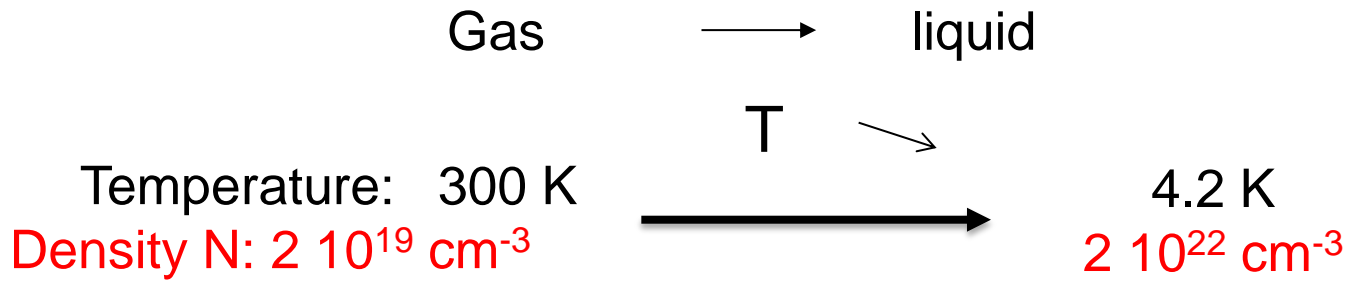
Optical Emission from Helium Cryoplasma

Discharge in dense fluids (liquids or high-pressure gases :1-100 bar)



$V \sim \text{kV DC}, I \sim 0,1-50\mu\text{A}$
 $P=0,1-100\text{mW},$
 gap distance $\sim 5-8 \text{ mm}$
 $R_{\text{tip}} \sim 0,1-2\mu\text{m}$

Corona-discharge



Goal:
 Determine $N_e, T_e, T, N_{\text{He}}$



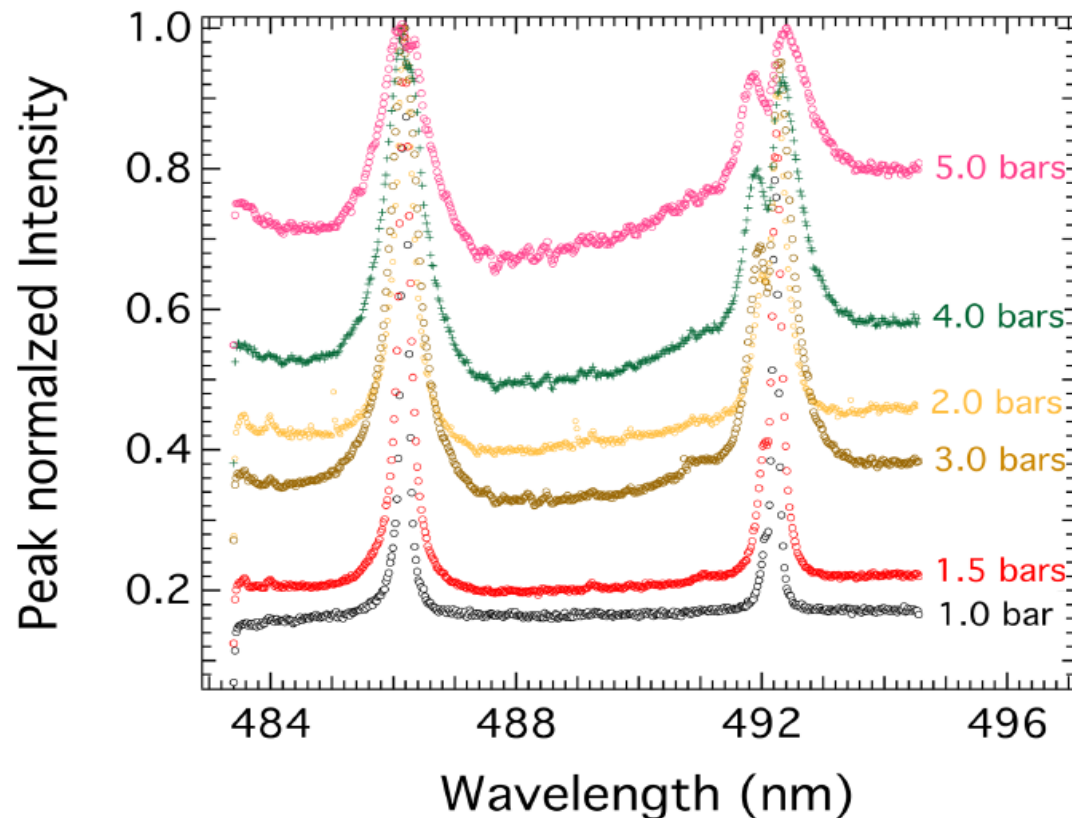
Code comparison code workshops

<http://plasma-gate.weizmann.ac.il/slsp/>



The 4th Spectral Line Shapes in Plasmas code comparison workshop – Baden –
March 20th to 24th, 2017

Corona discharge in helium 300 K





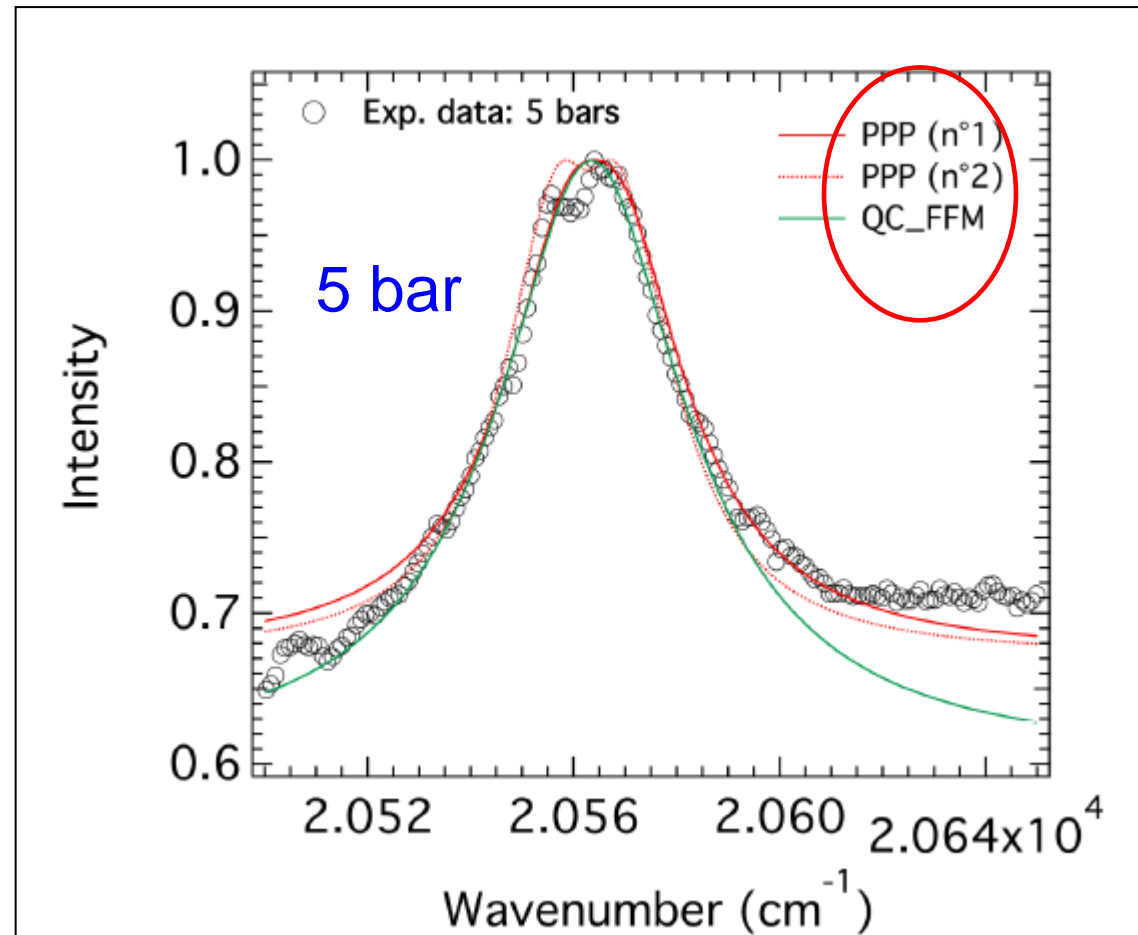
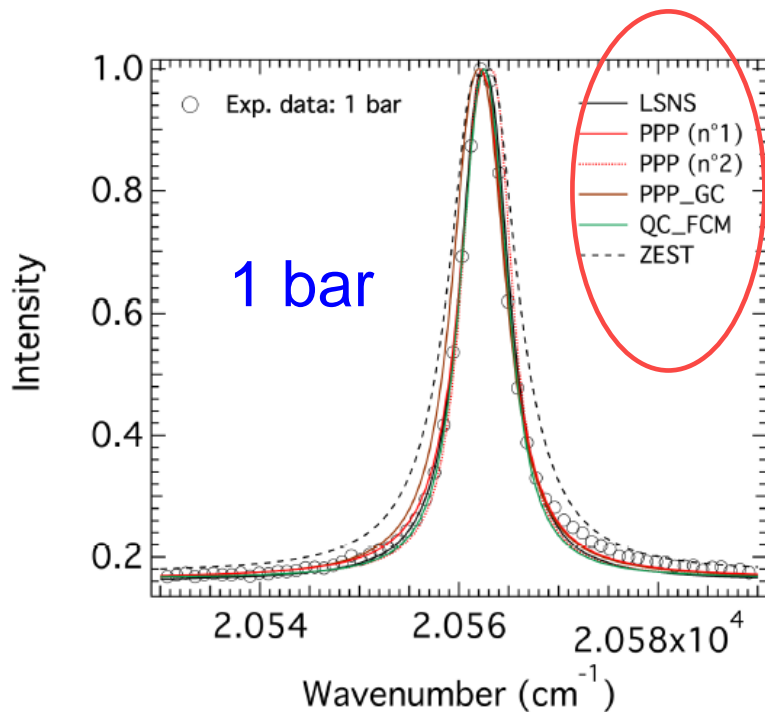
Code comparison code workshops

<http://plasma-gate.weizmann.ac.il/slsp>



Comparison of the FWHM of the H- β Line

300 K





H- β Line in a Corona Helium Plasma: A Multi-Code Line Shape Comparison

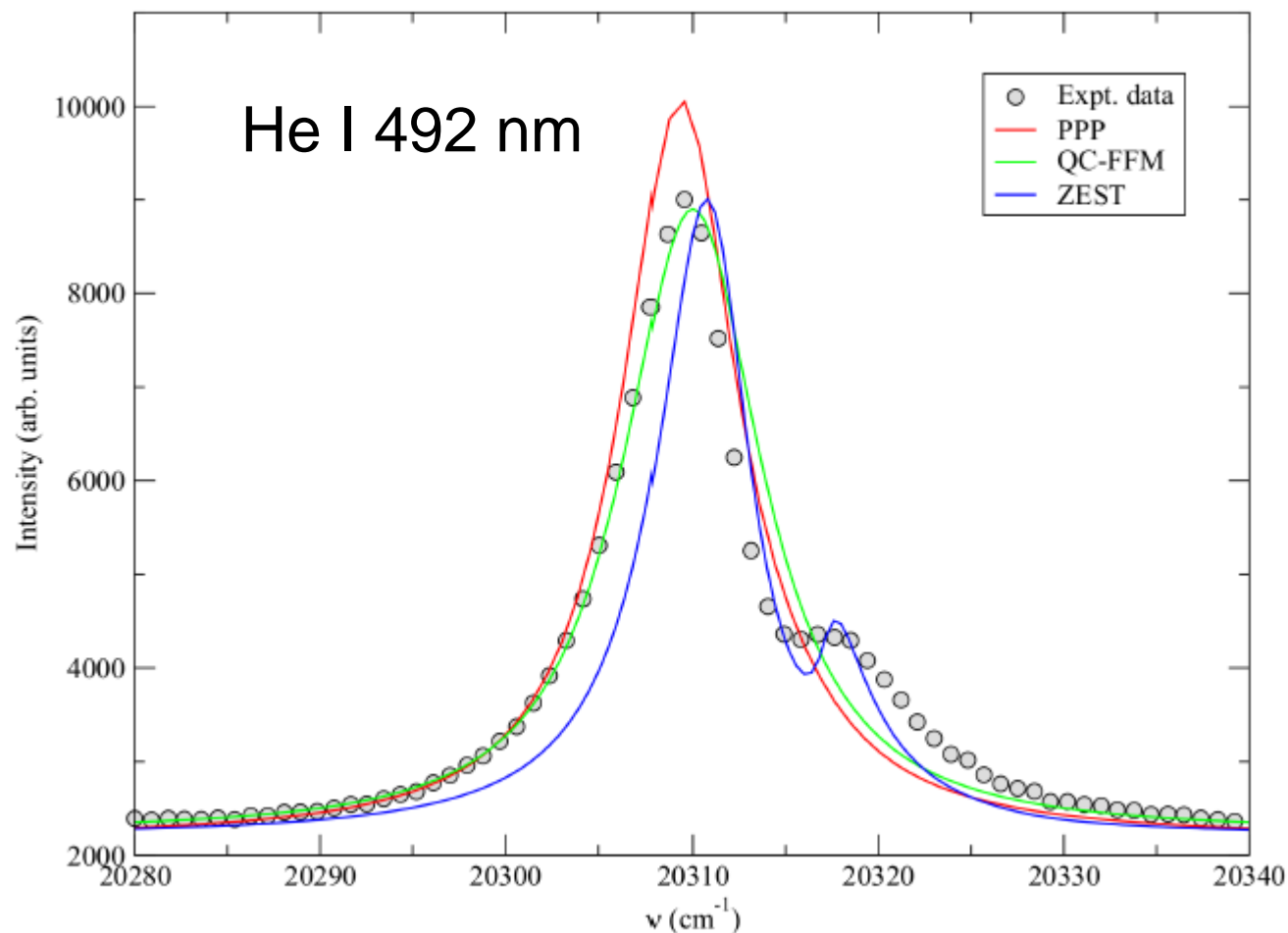
Table 3. The electron densities (in units of 10^{15} cm^{-3}) as inferred from the fit of the experimental H- β spectra by the contributing codes. P is the pressure in units of bars.

Case n ^o	P	LSNS	PPP (n ^o 1)	PPP (n ^o 2)	PPP_GC	QC_FFM	ZEST
1	1	0.5	0.15	0.26	0.18	0.8	1.2
2	1.5	1.1	0.3	0.58	0.38	2.2	2.7
3	2	-	0.55	1.0	1.3	4.7	-
4	3	-	0.9	2.0	-	10.0	-
5	4	-	1.3	2.8	-	15.0	-
6	5	-	1.9	3.8	-	27.0	-

RR Sheeba, M Koubiti, N Bonifaci, F Gilleron, C Mossé... -
Atoms **2018**, 6(2), 29; <https://doi.org/10.3390/atoms6020029>



Broadening of the Neutral Helium 492 nm Line in a Corona Discharge: Code Comparisons



1.5 bar 300 K

RR Sheeba, M Koubiti, N
Bonifaci, F Gilleron, JC
Pain... -
Atoms **2018**, 6(2), 19;
doi:[10.3390/atoms6020019](https://doi.org/10.3390/atoms6020019)



A New Procedure to Determine the Plasma Parameters from a Genetic Algorithm Coupled with the Spectral Line-Shape Code PPP



Table 5. Results of the fitting GA analysis of the H- β line. n_e : electron density; T_e : electron temperature; $\Delta\lambda_{VDW}$: van der Waals width; $\Delta\lambda_{ins}$: Gaussian width.

	Pressure (bar)	n_e (cm ⁻³)	T_e (10 ⁴ K)	$\Delta\lambda_{VDW}$ (nm)	$\Delta\lambda_{ins}$ (nm)
H β	1	10 ¹⁴	1.23	7.2 × 10 ⁻²	8.0 × 10 ⁻²
	2	8 × 10 ¹⁴	1.17	15.2 × 10 ⁻²	8.0 × 10 ⁻²
	3	1.85 × 10 ¹⁵	1.21	24.2 × 10 ⁻²	8.0 × 10 ⁻²

≠

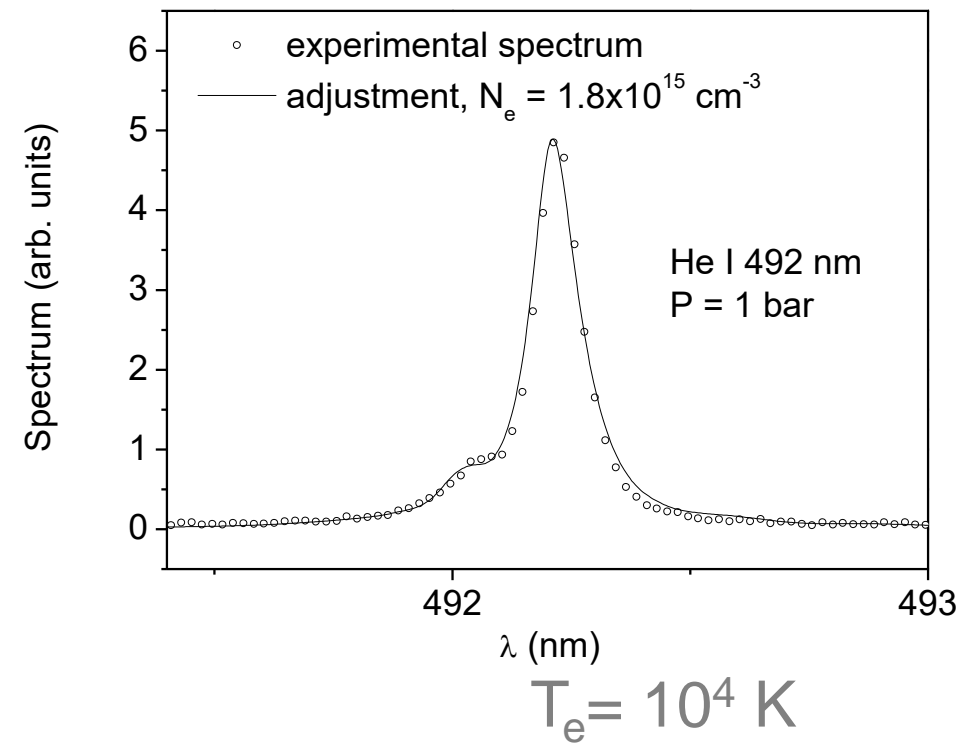
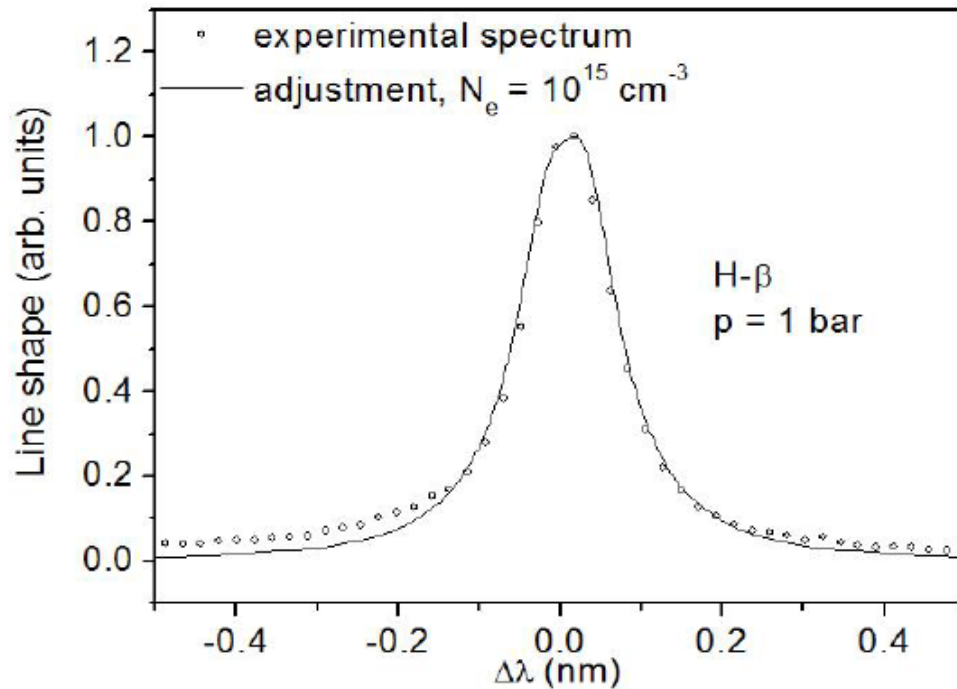
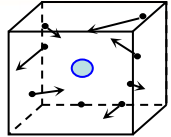
Table 6. Results of the fitting GA analysis of the He I 492 nm line.

	Pressure (bar)	n_e (cm ⁻³)	T_e (10 ⁴ K)	$\Delta\lambda_{VDW}$ (nm)	$\Delta\lambda_{ins}$ (nm)
492 nm	1	10 ¹⁵	1.21	2.93 × 10 ⁻²	8.0 × 10 ⁻²
	2	3.96 × 10 ¹⁵	1.16	5.82 × 10 ⁻²	8.0 × 10 ⁻²
	3	8 × 10 ¹⁵	1.16	9.7 × 10 ⁻³	8.0 × 10 ⁻²

Electron number density : N_e

Computer simulation method

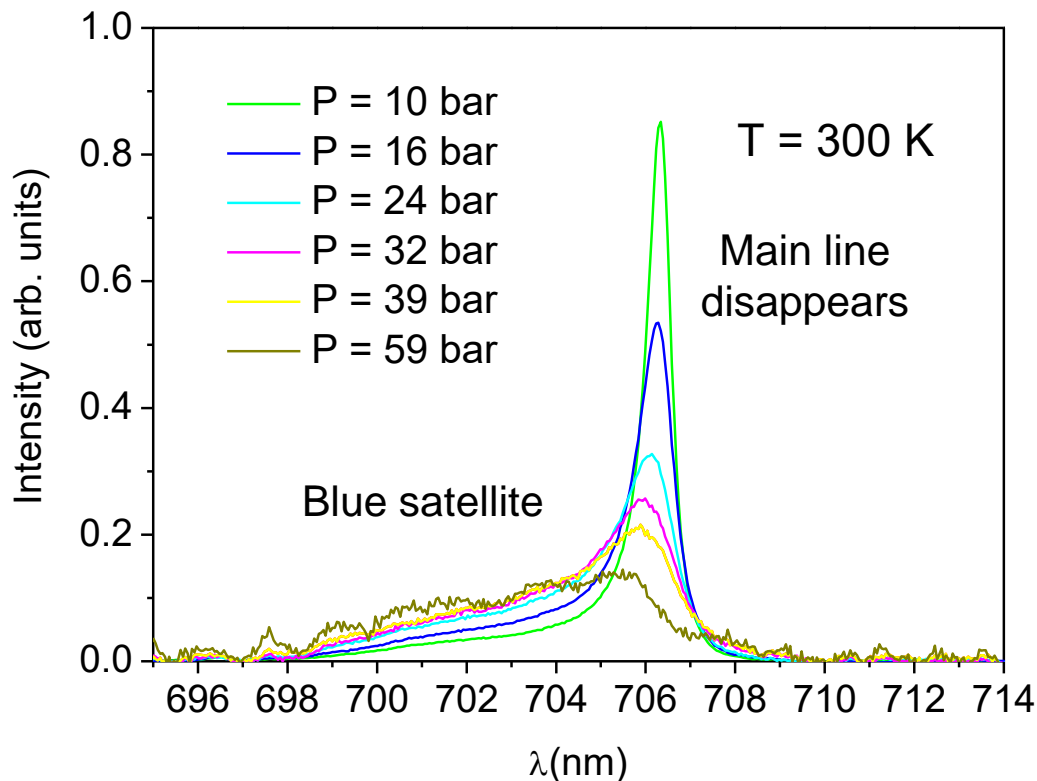
P = 1 Bar



Line Shape Modeling for the Diagnostic of the Electron Density in a Corona Discharge

Neutral Perturbers Density : N_{He}

300 K (P) 706 nm ($^3S-^3P$)



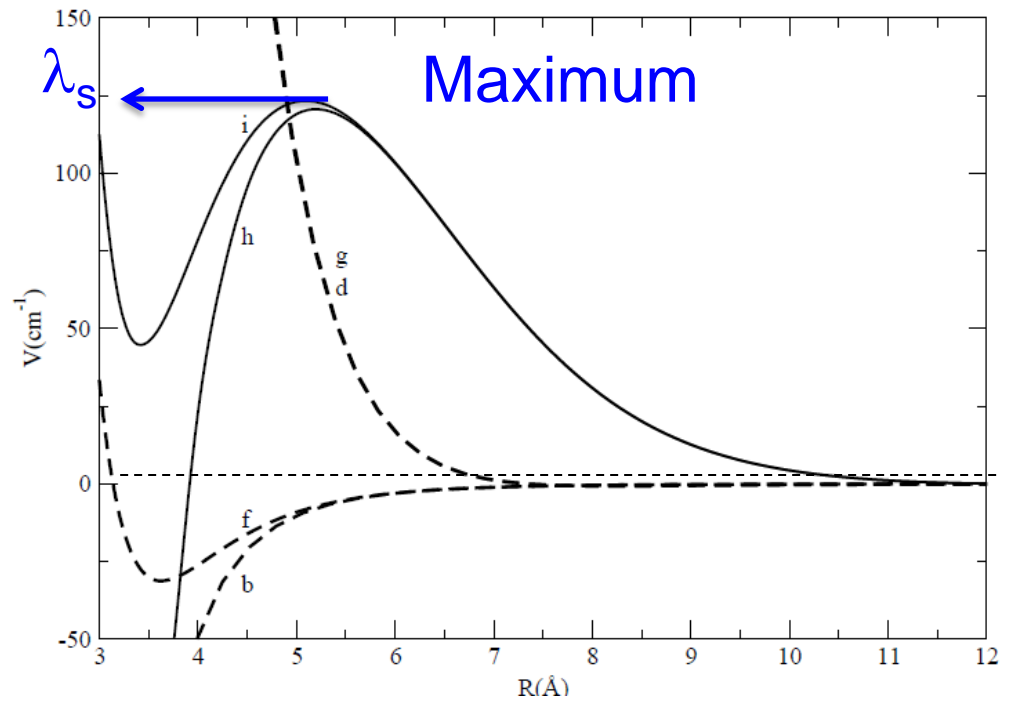
Fourier Transform of the dipole autocorrelation function

$$\phi(\tau) = e^{(-N_{He}g_{\alpha}(s))}$$

$$g_{\alpha}(s) = \frac{1}{\sum_{e,e'}^{(\alpha)} |d_{ee'}|^2} \sum_{e,e'}^{(\alpha)} \int_0^{+\infty} 2\pi\rho d\rho \int_{-\infty}^{+\infty} dx \tilde{d}_{ee'}[R(0)] [e^{\frac{i}{\hbar} \int_0^s dt V_{e'e}[R(t)]} \tilde{d}_{ee'}^*[R(s)] - \tilde{d}_{ee'}[R(0)]]$$

Neutral Perturbers Density : N_{He}

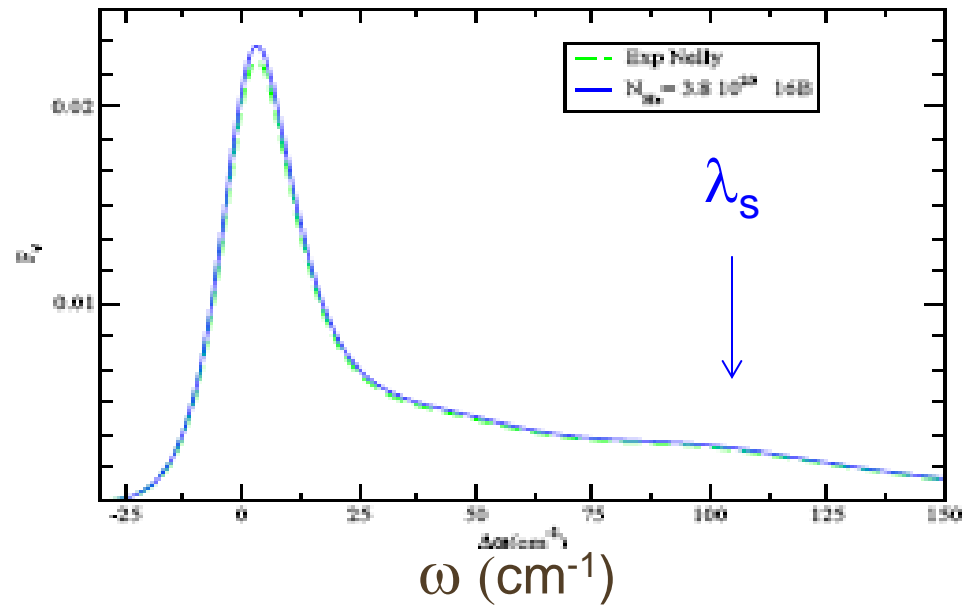
He*-He Potential



N ALLARD, et al EPL 88 (2009) 53002
 N ALLARD, et al EPJ D 61 (2011) 365-372

Comparison between experiment and theory

16 Bar



$$N_{per} = 3.8 \cdot 10^{20} \text{ cm}^{-3}$$

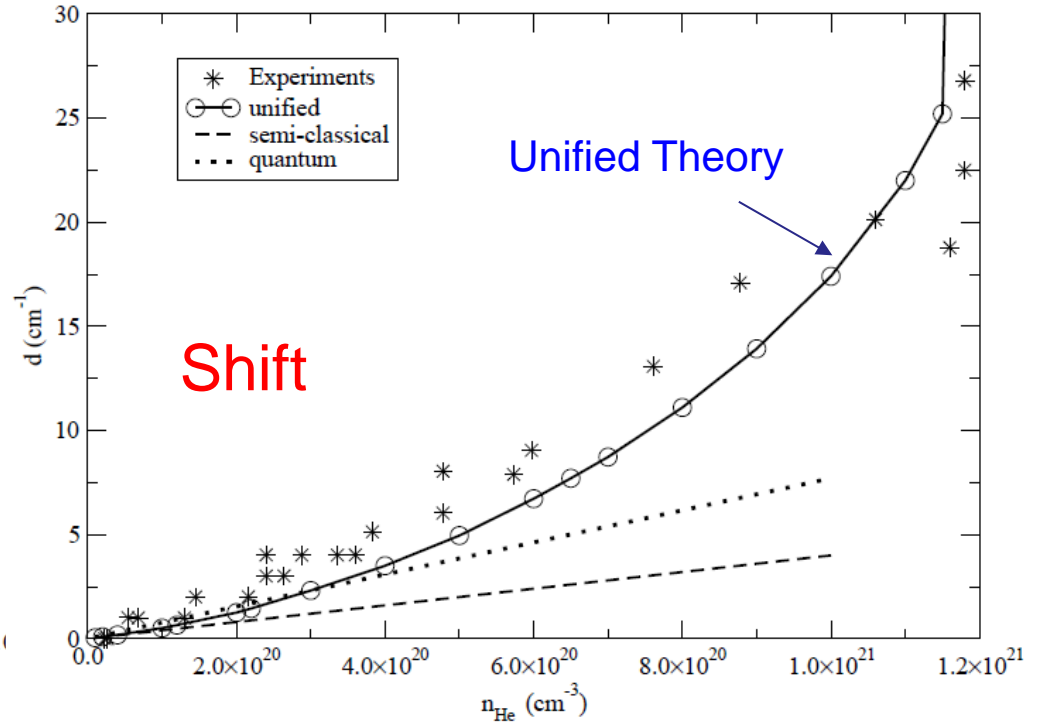
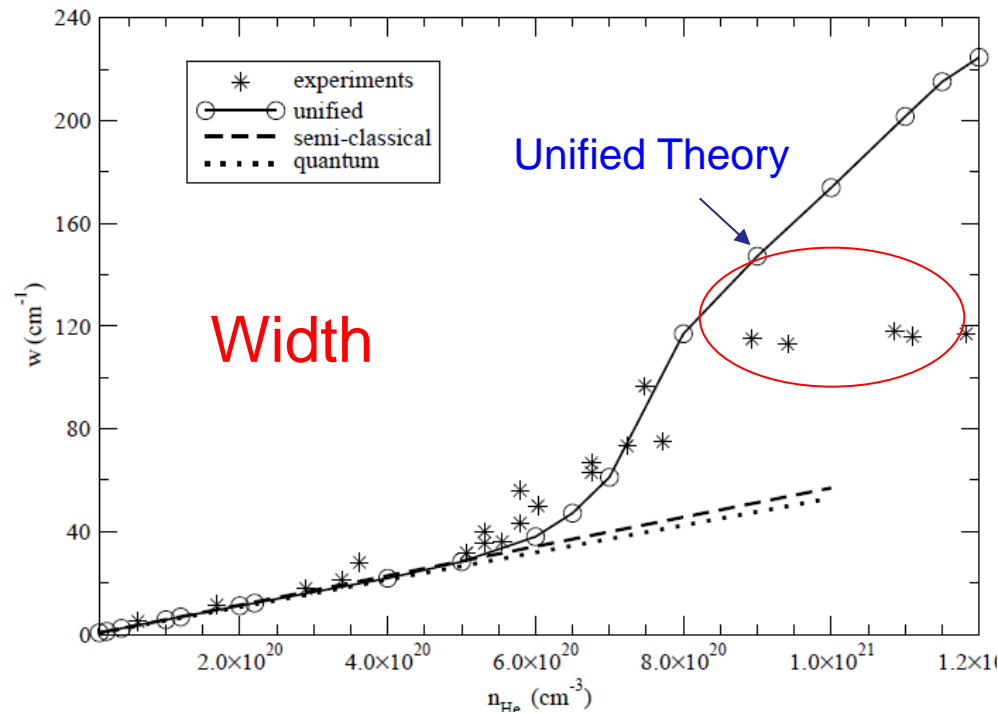
Results for He line 706 nm ($^3S-^3P$)
 at 300 K

Neutral Perturbers Density : N_{He}

300 K (P)

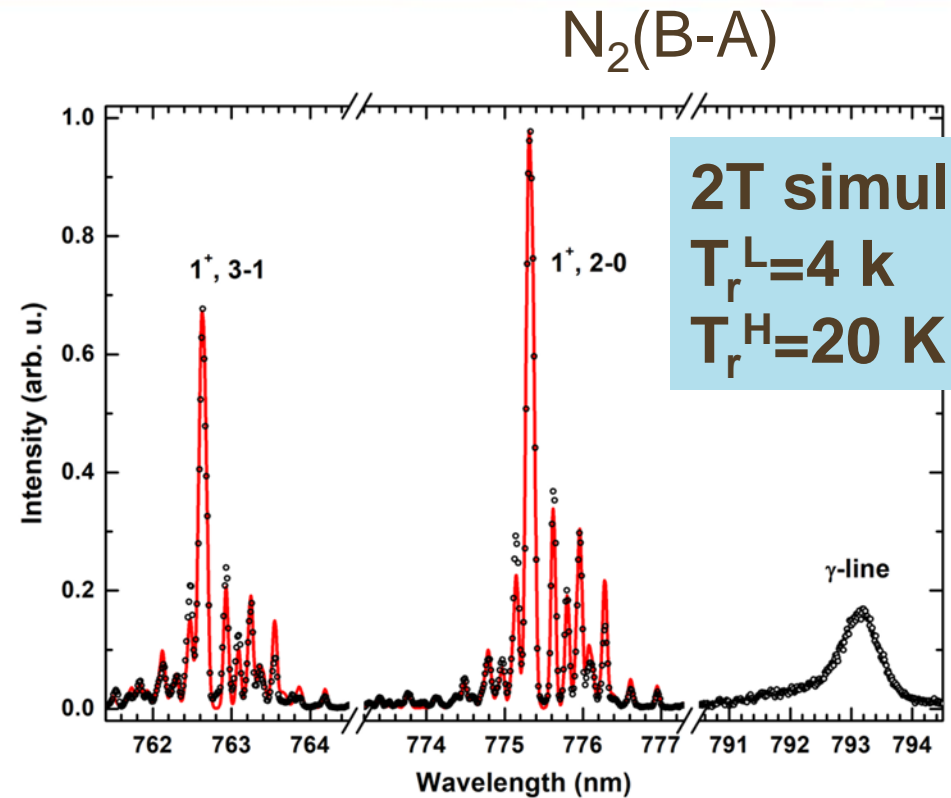
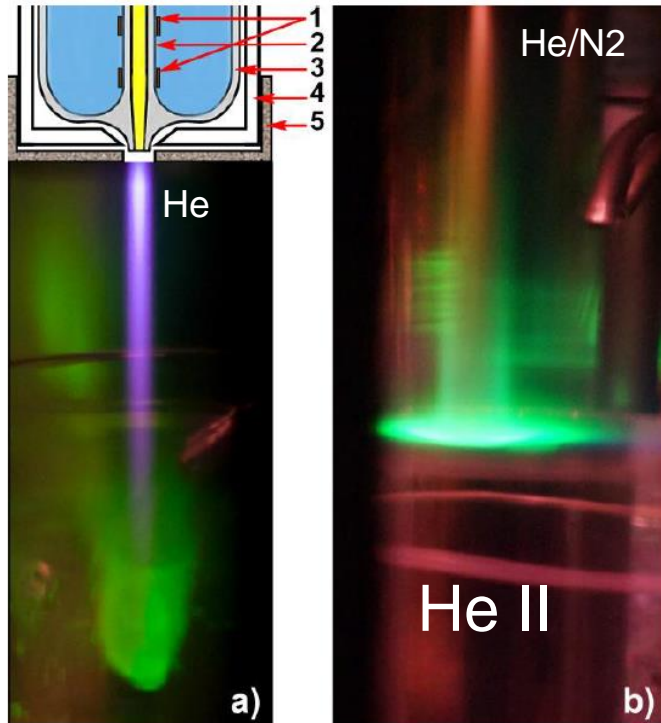
706 nm

Comparison between experiment and theory



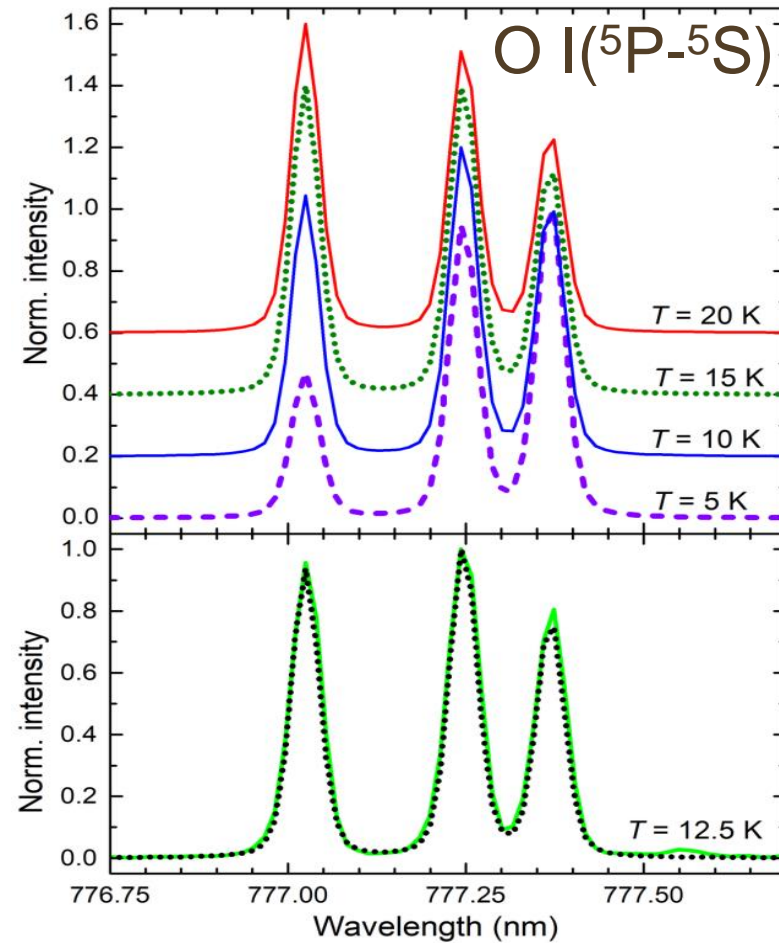
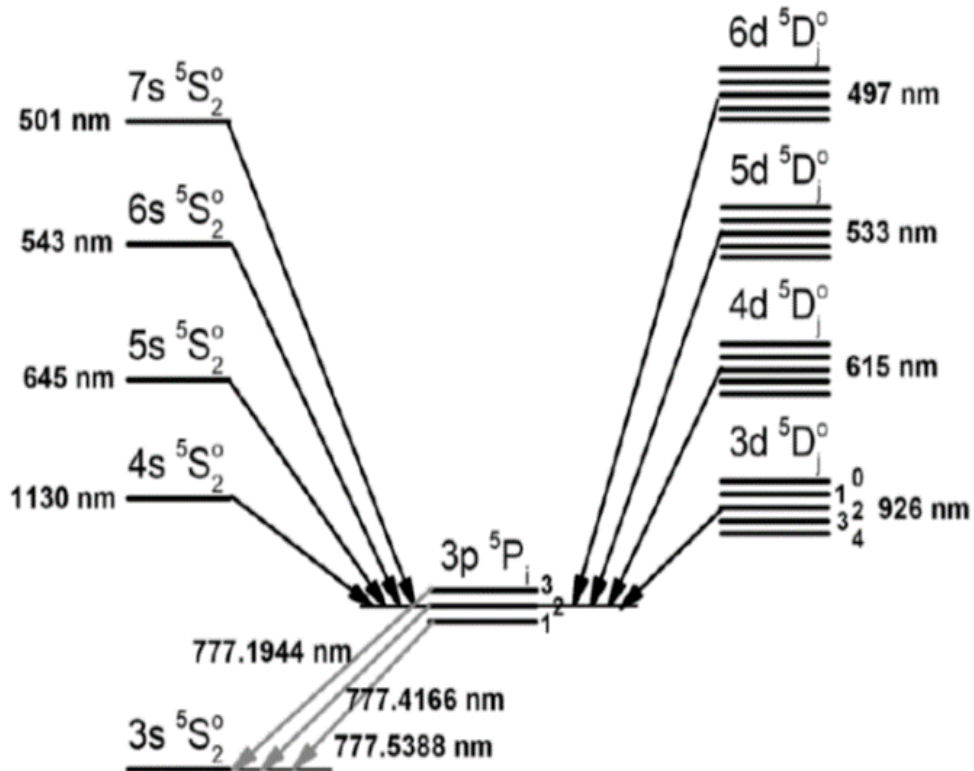
Discrepancy observed at high pressures

Cold helium jet excited by electrical discharges



$$[N_J] \propto (2J + 1) \left[\exp\left(-\frac{E_J}{kT_r^L}\right) + R\left(\frac{T_r^L}{T_r^H}\right) \exp\left(-\frac{E_J}{kT_r^H}\right) \right]$$

Cold helium jet excited by electrical discharges



Cold helium jet excited by electrical discharges

gas	probe	top	middle	bottom
pure He [N ₂]/[He] = 1/10000	O atom			12.5
	O atom	70	36	23
	N ₂ (1 ⁺ , 2-0) PGOPHER	42±10.5	30±7.5	18±4.5
	N ₂ (1 ⁺ , 2-0) 2-T*	20-100	18-70	8-70
[N ₂]/[He] = 1/400	N ₂ (1 ⁺ , 2-0) 2-T			4-20
	N ₂ (1 ⁺ , 2-0) PGOPHER			13.2±2
	N ₂ (1 ⁺ , 3-1) 2-T			4-25
	N ₂ (1 ⁺ , 3-1) PGOPHER			14±2.1
[N ₂]/[He] = 1/200	N ₂ (IRA, 8-3) PGOPHER		33±6.6	10.5±2.1
	N ₂ (1 ⁺ , 2-0) PGOPHER	67±6.7	39±3.9	13.6±1.4
	N ₂ (1 ⁺ , 2-0) 2-T	30-120	14-60	5-20

Interaction Physical classification

Stark (*literature*)
Van der Waals ($-C_6/r^6$)
Resonant ($\pm C_3/r^3$)

Potentiel ab initio
Code MOLPRO
<http://www.molpro.net>

Spectral line Profile

Classical theory

- Unified theory
- Impact approximation
- Quasistatic approximation

Quantum treatment

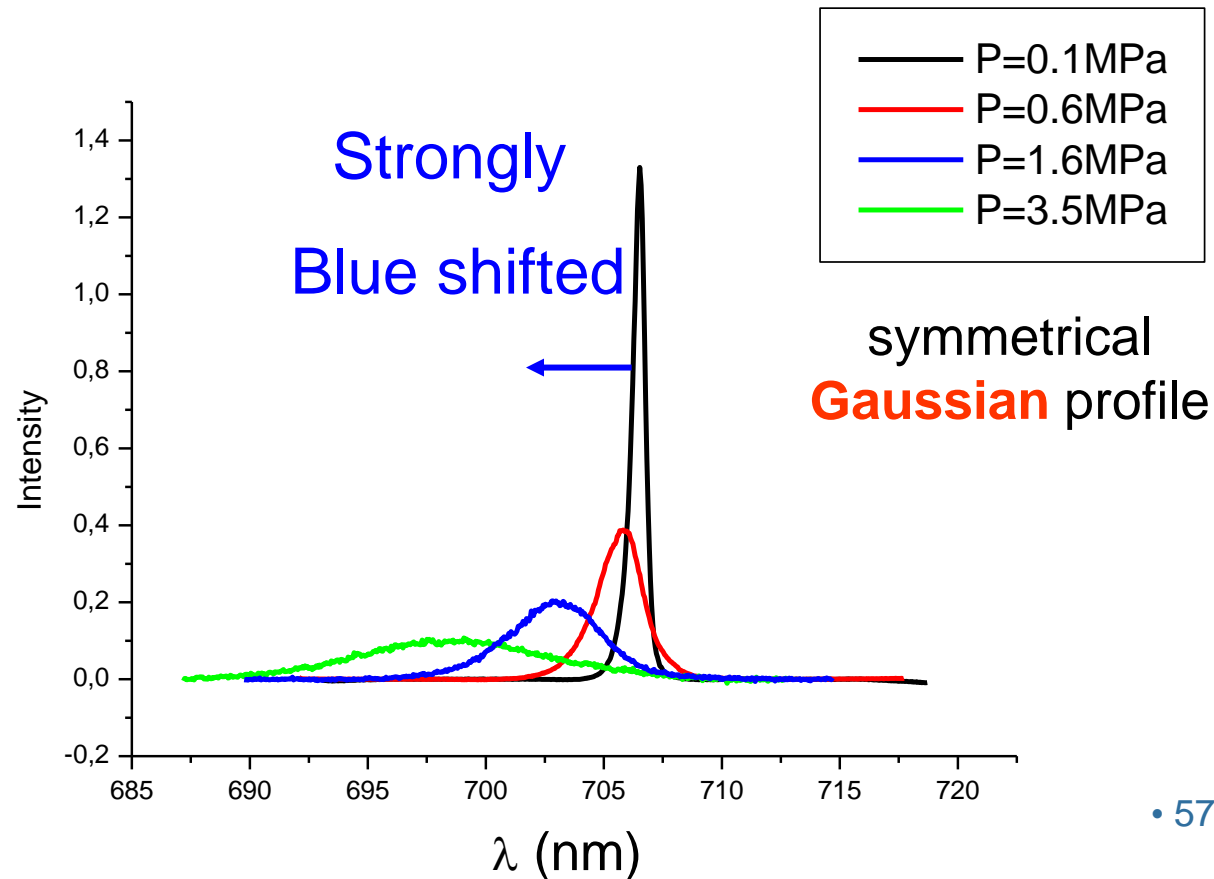
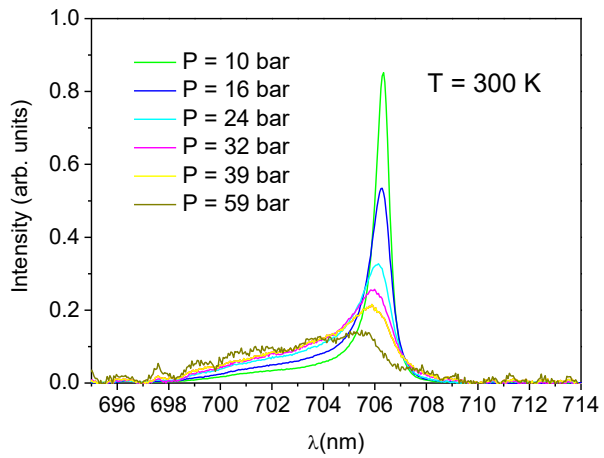
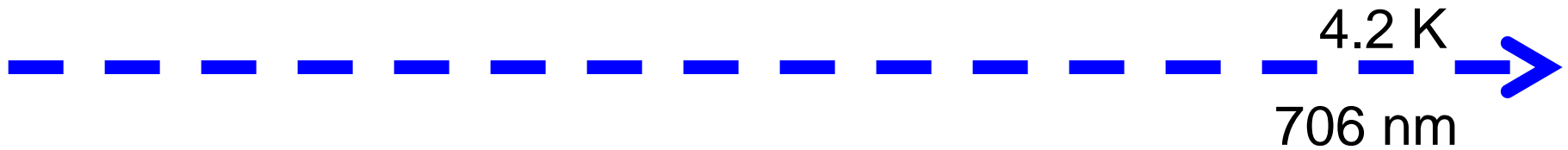
PIIM Marseille
Weizmann Institute of Science, Israel;
Valladolid Spain

Spectral Line Shapes in Plasmas code
comparison workshop

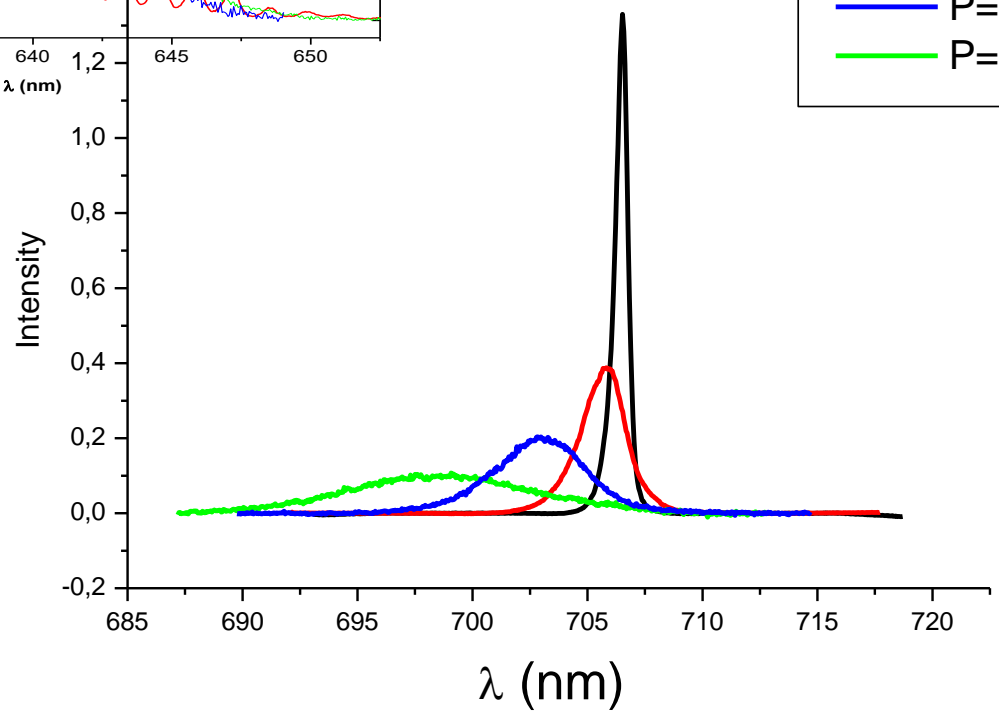
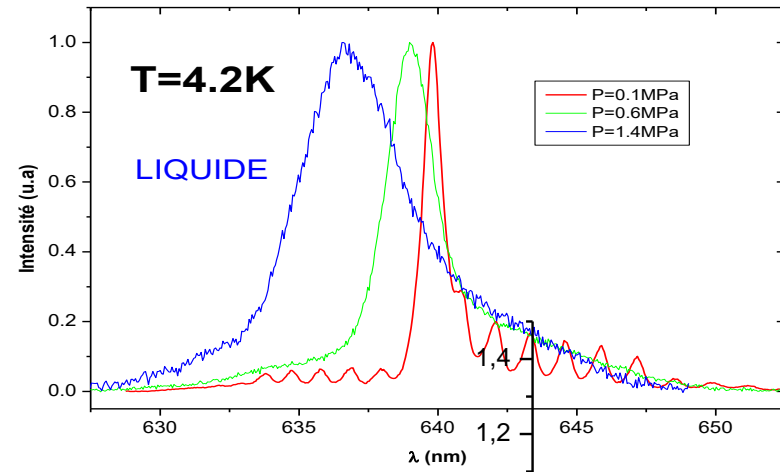
Thank you for your attention



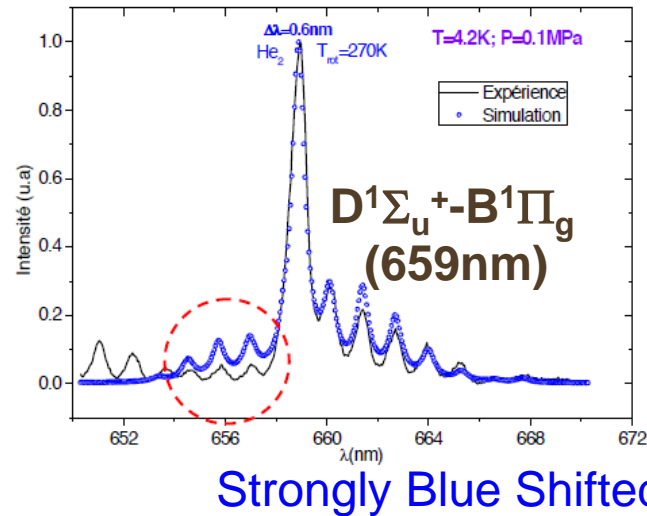
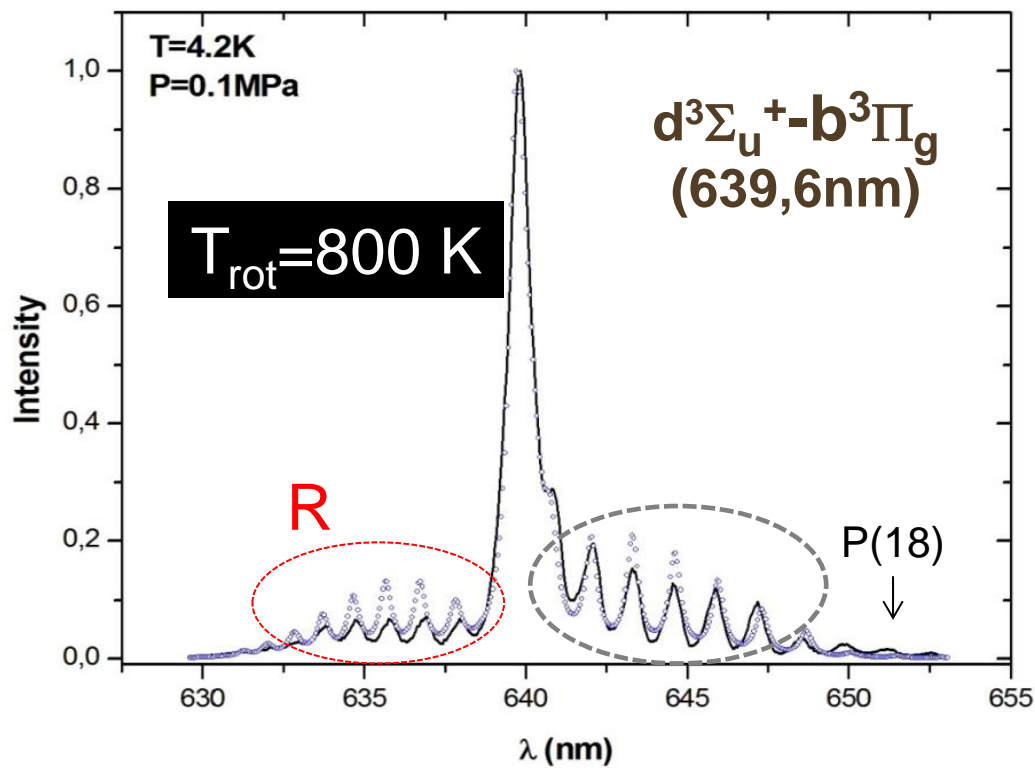
Neutral Perturbers Density : N_{He}



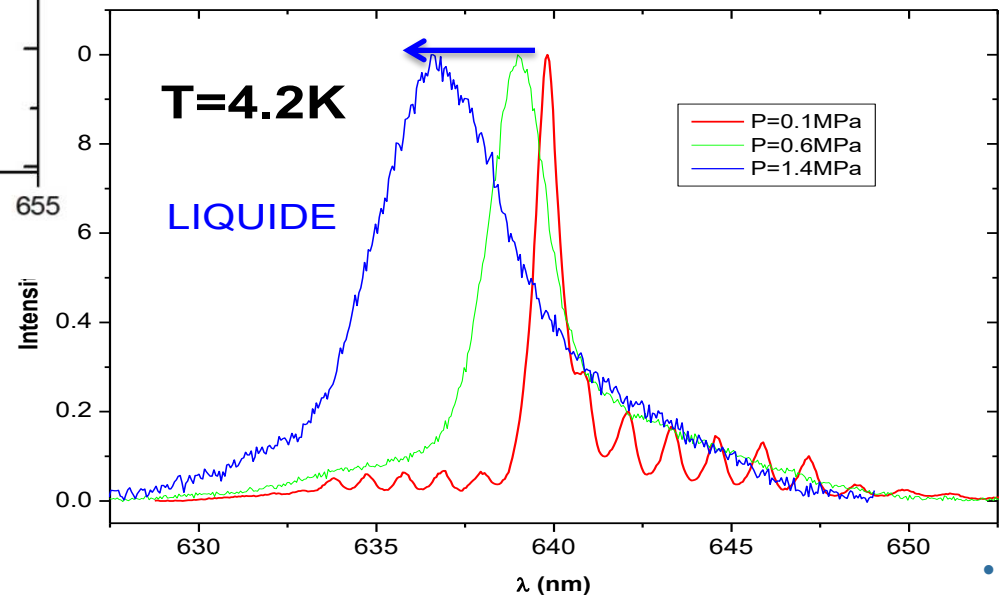
Interpretation ? 4.2 K



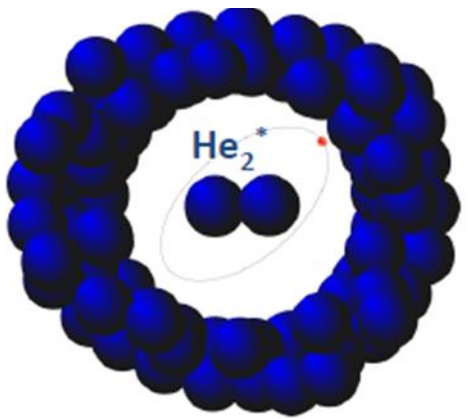
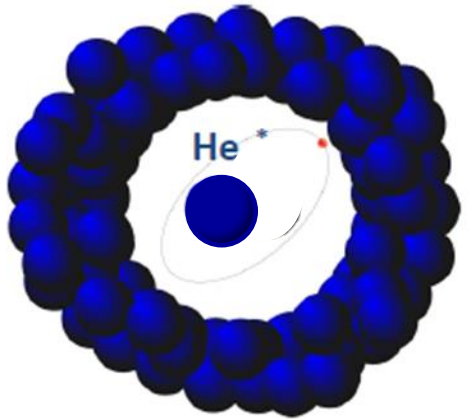
Temperature : Rotational temperature measurements



No boltzmann distribution
High degree of rotational excitation



He* He₂* Rydberg electron



Interpretation:

Microscopic void around the He*3s and He₂*3d



Repulsion between Rydberg e⁻ and surrounding atoms in the ground state forms bubble

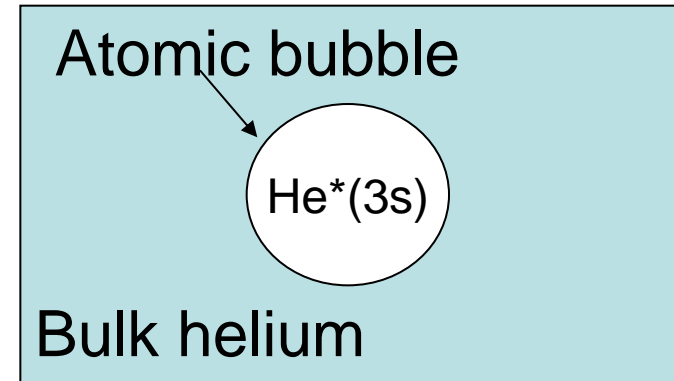
New autocorrelation function with « bath » interaction

$$\Phi(\tau) = \exp\left(-\int \left(1 - e^{-i\Delta V_{fi}(r)t/\hbar}\right) \rho_i(r) d^3r\right)$$

Difference pair potential between the states corresponding to the emission line

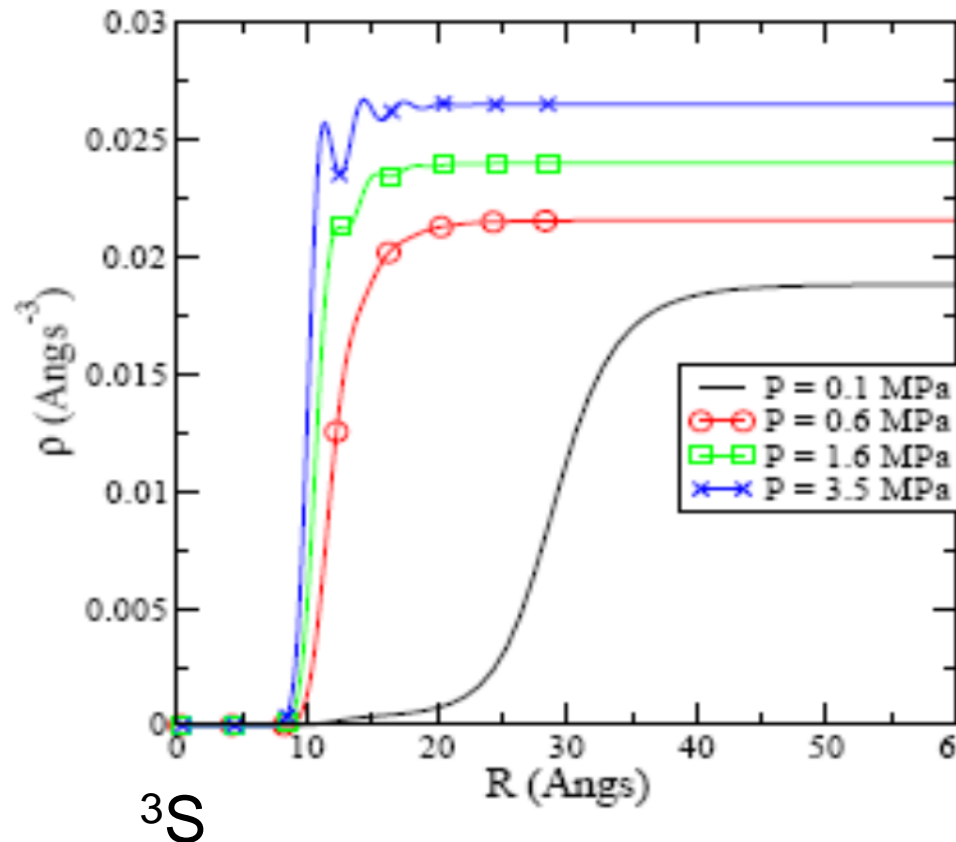
Molpro code

Liquid density in the electronic ground state around 3s calculated using Bosonic Density Functional Theory DFT



Liquid density around $\text{He}^*(3s^3S)$

Liquid density around $3s^3S$ calculated using DFT



35 bar Phys. Rev. A 85 042706 (2012).

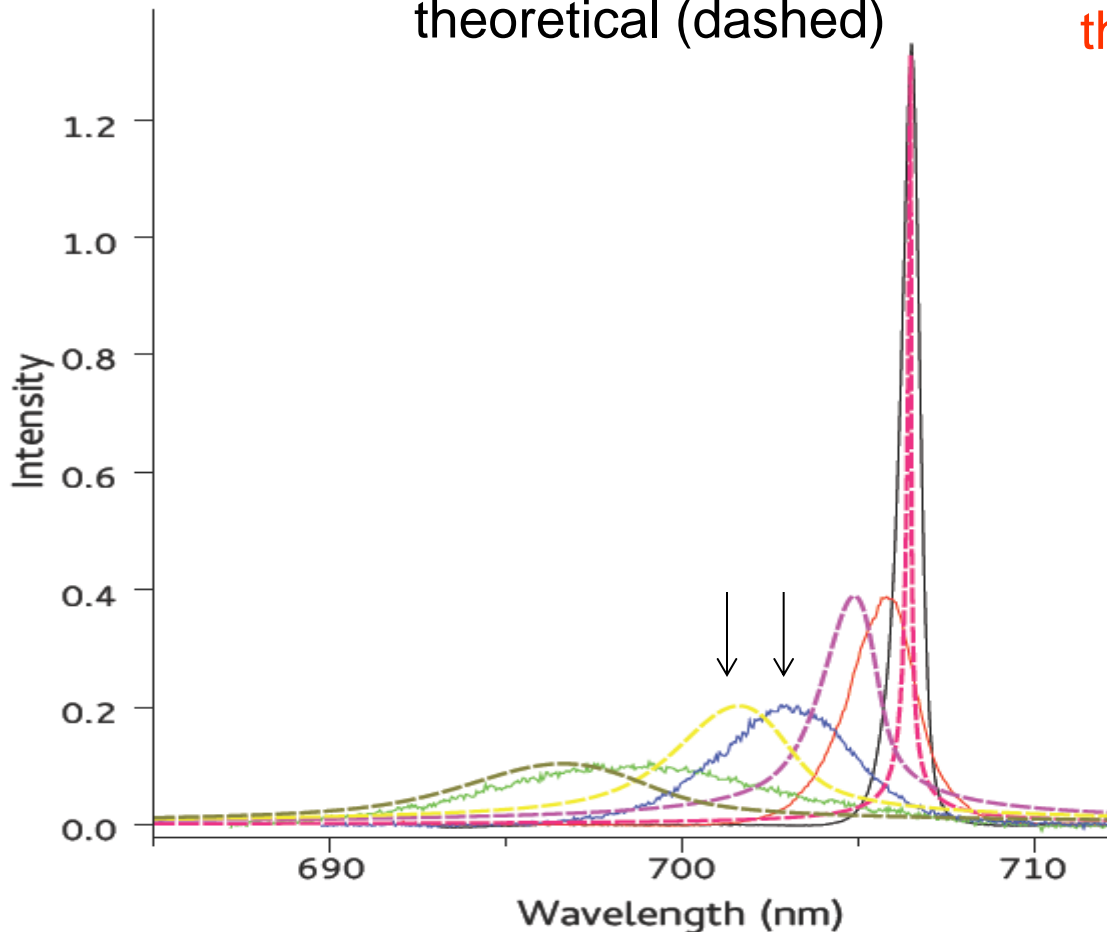
1 bar

Bubble Radius (R_b) depends on applied pressure (P).

Empty cavity around excited atom (emitter)

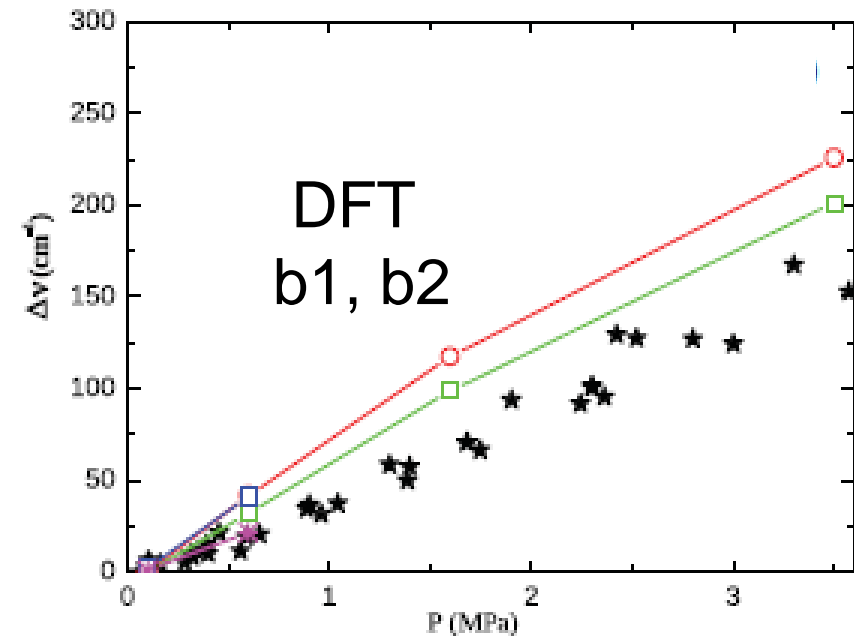
706.5 nm He* line ($^3S-^3P$)

Experimental (continuous) vs theoretical (dashed)



the line position is extremely sensitive to the He*(3s) - He pair potential

Line shift



Electron number density : N_e

300 K (P)

150 K

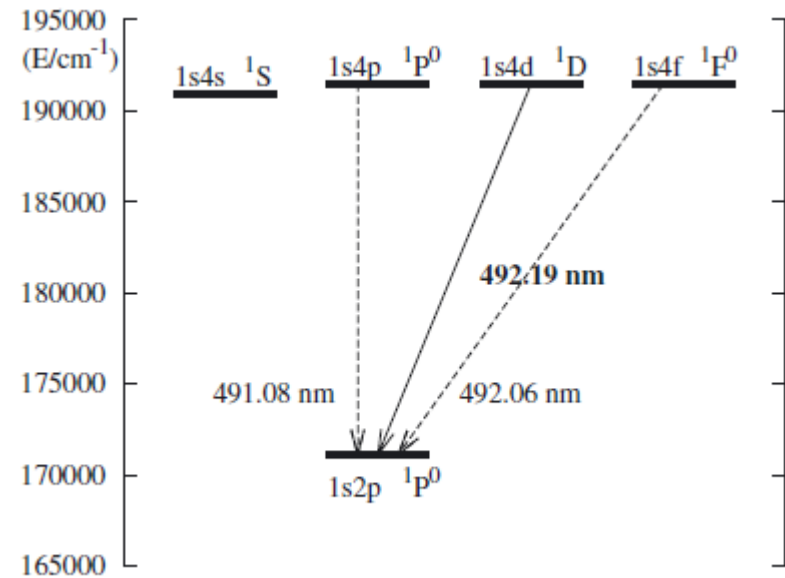
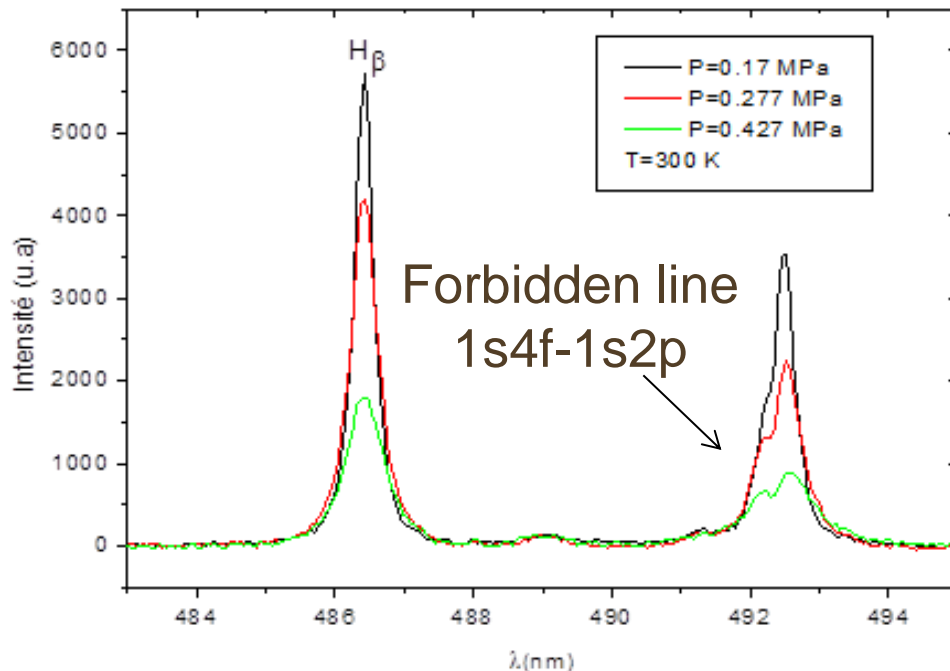
11 K

4.2 K(P)

H α : 656 nm
 H β : 486 nm
 He I : 492 nm

He 492 nm

300 K



Historical development

Impact approximation Phase shift

Weisskopf (1932), Lindholm (1941), Foley (1946)

$$\omega(t) = \omega_0 + \frac{d\eta}{dt}$$

Quasistatic approximation

Holtmark (1919), Kuhn and Margenau (1937),

$$\omega = \omega_0 + \frac{\Delta V(r)}{h}$$

Line shape formalism based on the Fourier transform of the autocorrelation function

$$P(\omega) = \frac{1}{\pi} \operatorname{Re} \int_0^{+\infty} \phi(\tau) \exp[i\omega\tau] d\tau \quad \phi(\tau) = \int_{-\infty}^{+\infty} e^{i(\eta(t) - \eta(t-\tau))} dt$$

Autocorrelation function (wave train)

The width of the Voigt profile $\Delta\lambda_v$ is approximated by equation where $\Delta\lambda_G$ and $\Delta\lambda_L$ are the Gaussian and Lorentzian FWHMs, respectively

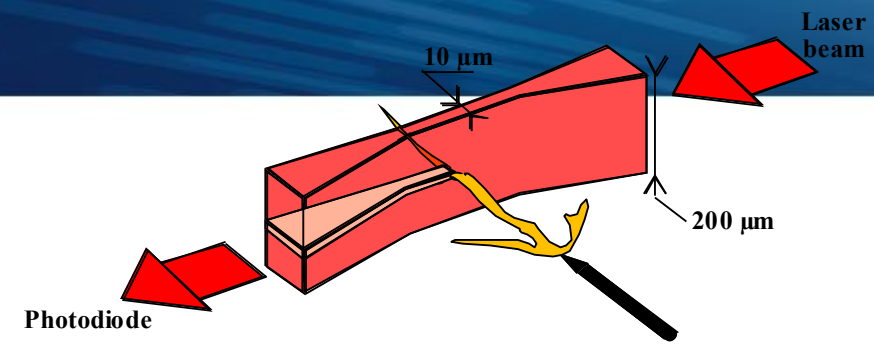
$$\Delta\lambda_v \approx \frac{\Delta\lambda_L}{2} + \sqrt{\frac{\Delta\lambda_L^2}{4} + \Delta\lambda_G^2}$$

Positive filamentary streamers in liquid nitrogen

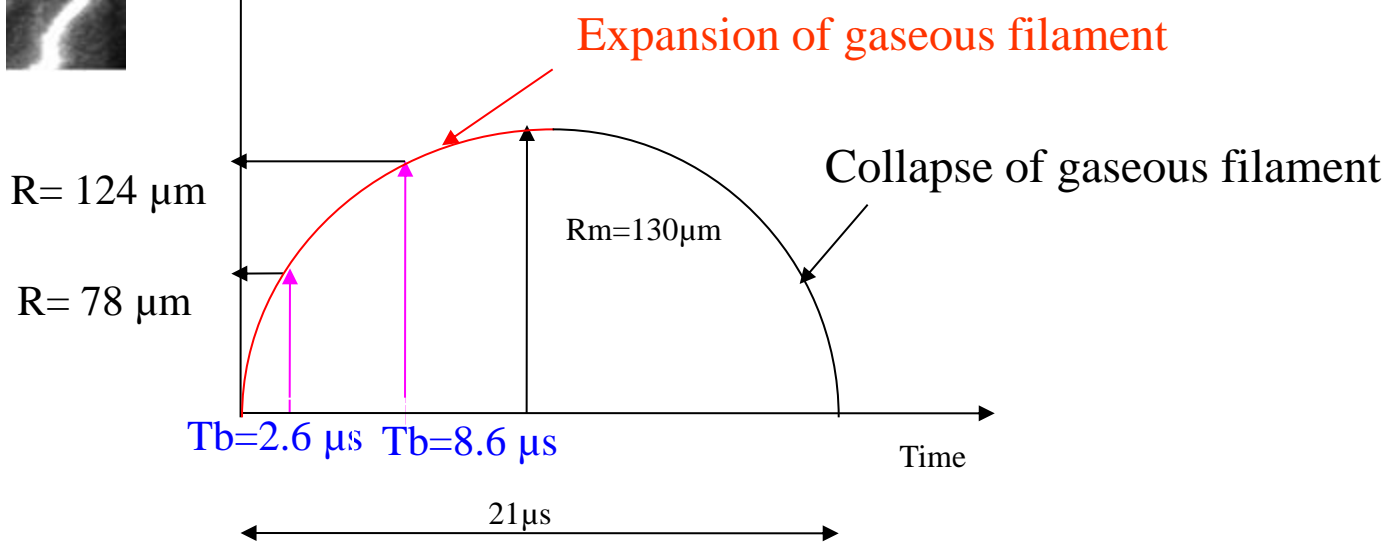
Re-illumination



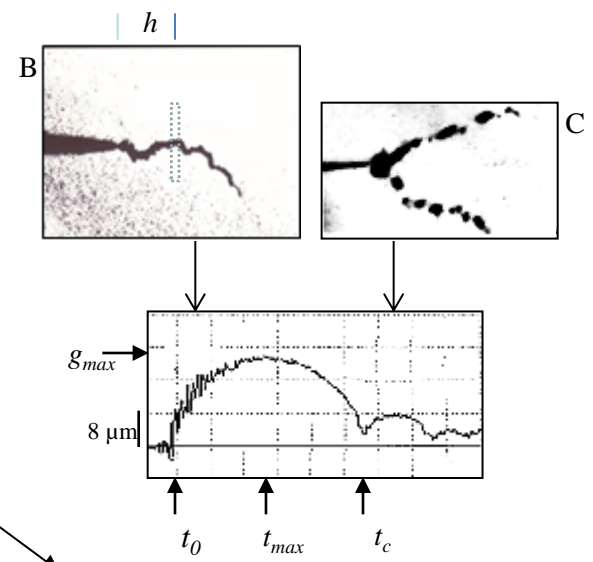
$N_g (2.6\mu s) > N_g (8.6\mu s) ?$



streamer channel radius



P Gournay and O Lesaint 1994



T_b → The plasma column has expanded N_g →

Neutral Perturbers Density : N_{He}

Unified semiclassical theory

4.2 K
706 nm

